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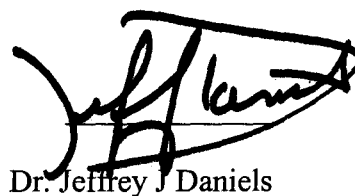
Senior Thesis

Ground Penetrating Radar: Antenna Effects and Patterns.

By
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Abstract

In the spring of 1998, 816 lines of Ground Penetrating Radar (GPR) data were recorded to determine the effects of antenna orientation on reflection data. The large amount of data collected allowed for the investigation of many variables that affect GPR data. One of the few variables that can actually be changed in field situations, (in other words not inherent to the target) is antenna orientation. The importance of different antenna orientations is demonstrated within. After the data was processed and put into visual form, comparisons could be made, and conclusions and generalizations were possible based upon them. The requirements for the detection of a target include the following: 1) a sufficiently strong input wave is needed, 2) the impedance contrast needs to be high enough for a reflection, 3) the target size needs to be sufficient for the burial depth, and 4) other objects must not interfere. The effects of target size, target type, burial depth, offset, and antenna orientation are shown. Polarization, and therefore antenna orientation, is shown to have a large affect on the resulting data quality. In most situations best results were obtained with the antennas oriented perpendicular to the traverse of the line.

Introduction

This study was undertaken, with the guidance of Dr. Daniels, in order to study the effects of different antenna variables on GPR data. A massive amount of data was collected; thirty-four lines were run for two target types (conductor and dielectric), of three sizes (2", 6", and 11" diameters), at two burial depths (1' and 2'), and with two antenna orientations (parallel and

perpendicular to traverse), for a total of 816 traverse lines of data. This provided ample data for the study of a number of factors. Target shape and orientation were not among these, because perfect spheres were used. However, by using a perfect sphere, the effects of polarization could also be studied. A uniform sphere gives the same reflection, for the same incident energy, in any direction. Any variations with respect to antenna orientation and offset, other than a steady increase in two way travel time with offset, must be due to polarization.

Section 1: GPR concepts

Ground Penetrating Radar is a relatively new shallow subsurface exploration tool, dating back no further than approximately 1970. It is based on the response of electromagnetic radiation to boundaries in the subsurface. The radiation does one or more of three things at a boundary; it is reflected, refracted, or diffracted. These boundaries are defined by an electrical properties (or impedance) contrast, which arises from conductivity, and permittivity variations. These contrasts show up in GPR records as anomalies. It is the identification, interpretation, and manipulation of these anomalies that is the key to determining the existence, depth and physical characteristics of a buried target.

The source for the electromagnetic radiation is a transmitting antenna. A commercially available GSSI 500 MHz antenna (with a SIR-10 control unit) was used for these experiments, but there is a wide range of antenna types, with each one designed for specific ground conditions. GPR antennas are generally wide band, and are identified by their center band frequency. A higher frequency antenna allows for greater resolution, and less penetration, while a lower frequency will go further into the earth at the cost of resolution. The properties of the ground can

not be changed, but the antenna characteristics can be manipulated to improve records. The antenna sends a pulse of radiation into the ground. However, before it even reaches the host rock, the signal is subject to interference from system electronics, internal coupling, and the electrical properties of the air-ground interface.

The electromagnetic wave propagates through the host material until it reaches an impedance contrast, at which point it is reflected (figure 1). An impedance contrast is a difference in electrical properties that causes electromagnetic energy to scatter. The strength of this reflection is proportional to the contrast in impedance. The reflected wave can travel back through the medium and be detected by a receiving antenna. The transmitting and receiving antennas can be separate (bistatic) or one antenna can be used for both transmitting and receiving (monostatic). The orientation of the antennas can be of great importance, as will be discussed later.

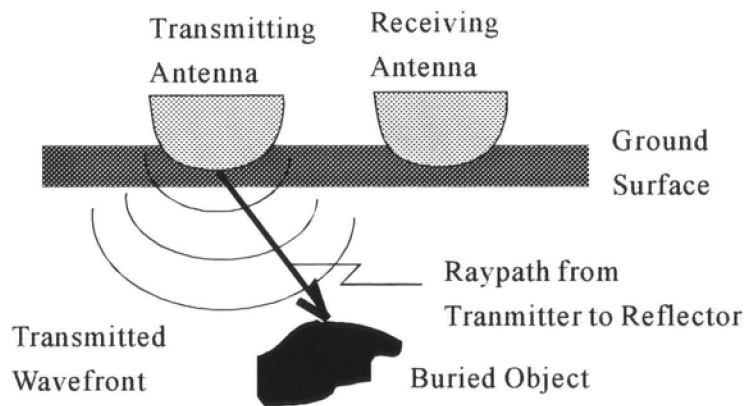
The reflections are recorded digitally over a certain time interval, which depends on the speed of the wave through the medium, or propagation velocity. A two way travel time is what is measured, where: $t_d = 2Z/V$

t_d is the two way travel time in nanoseconds

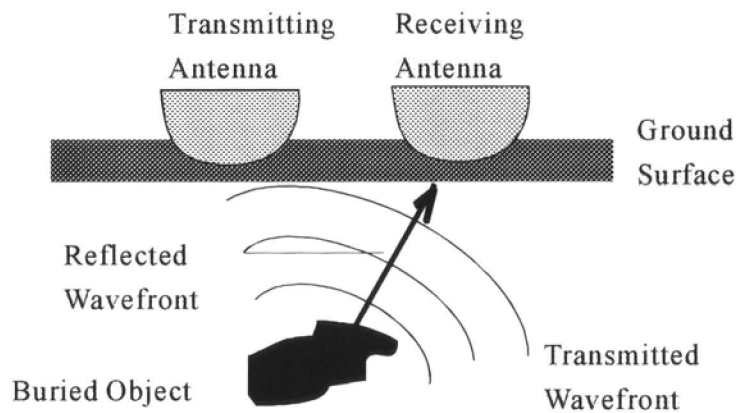
Z is depth to target in meters

V is propagation velocity in meters per second

The dominant factor allowing for propagation is the relative electric permittivity. A low relative permittivity yields a high velocity, and a high relative permittivity yields a lower velocity.



(a) Radar wave transmitted as a cylindric spreading wave.



(b) Reflected wave from a point on a buried object.

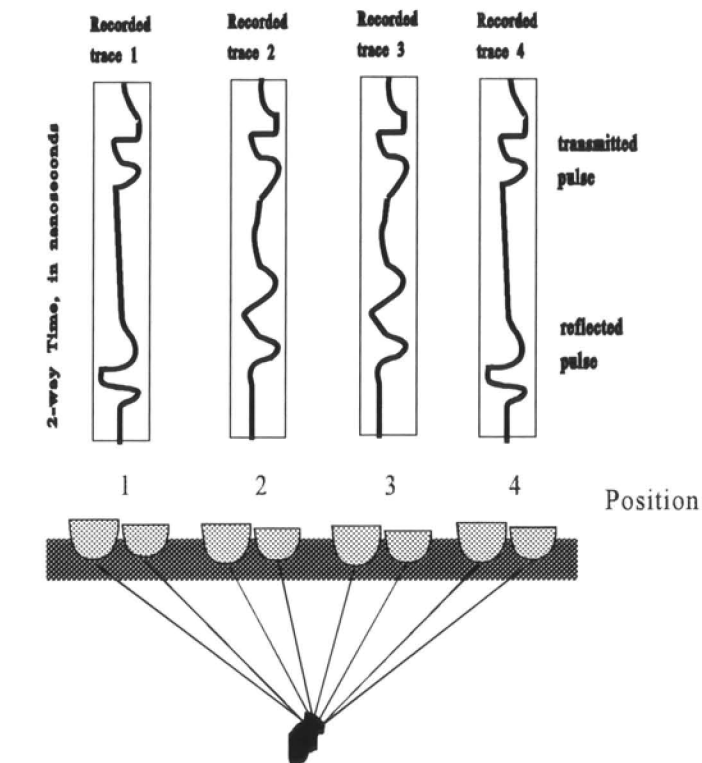
Figure 1. The GPR reflection process. The wavefront spreads out from the transmitting antenna and reflects from the buried object, before it is detected by the receiving antenna. (From Daniels, 1994)

One set of a transmitted and received signal, with reflection if present, is called a trace. By assigning a shade of gray to amplitude ranges and placing successive traces of a line side by side, a gray-scale cross section is generated. This process is illustrated in figures 2 and 3. Displaying successive lines side by side yields a three dimensional time image of the subsurface as shown in figure 4. Noise and clutter are also present on the records, and all GPR data needs to be interpreted to separate reflections from noise. Noise and clutter can either mask a reflection, or appear to be something that is not there. Noise is a signal from outside phenomena (like radio interference), clutter is reflected energy from targets other than the target of interest. Filtering and stacking of data can often overcome this.

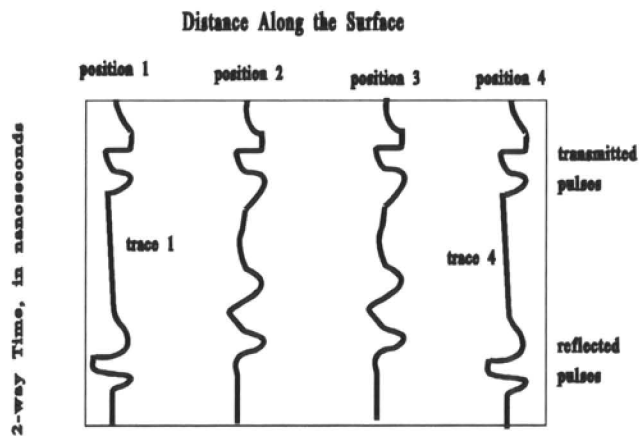
In order for the system to detect an object, the following conditions must be met: 1) the transmitted wave must be strong enough to go to the buried object and return to the surface, 2) the impedance contrast must be high enough, 3) the object must be large enough to be detected at that depth, and 4) Other objects must not interfere.

Section 2: Fundamentals of Polarization

Propagation and polarization control how and if electromagnetic radiation gets from the source, into the host material, to the target, and back to the receiver. Not only does the energy have to return to the receiver, but it must do so in the right orientation. If not, the reflection may appear exceptionally weak, or may not show up at all. This is where polarization becomes important. Polarization is the alignment of electromagnetic vibrations, or waves, in preferential directions. Radiation can be linear or elliptically polarized. If a unit vector is assigned to the electric field generated by the radiation, then the path that this vector follows as the wave propagates defines the polarization orientation. If it stays in one plane it is said to be plane



(a) Single traces recorded at different antenna locations.



(b) Resulting 4 trace GPR record, or cross section.

Figure 2. The process of combining traces, recorded at even spacings on the surface, to form a GPR record. (From Daniels, 1994)

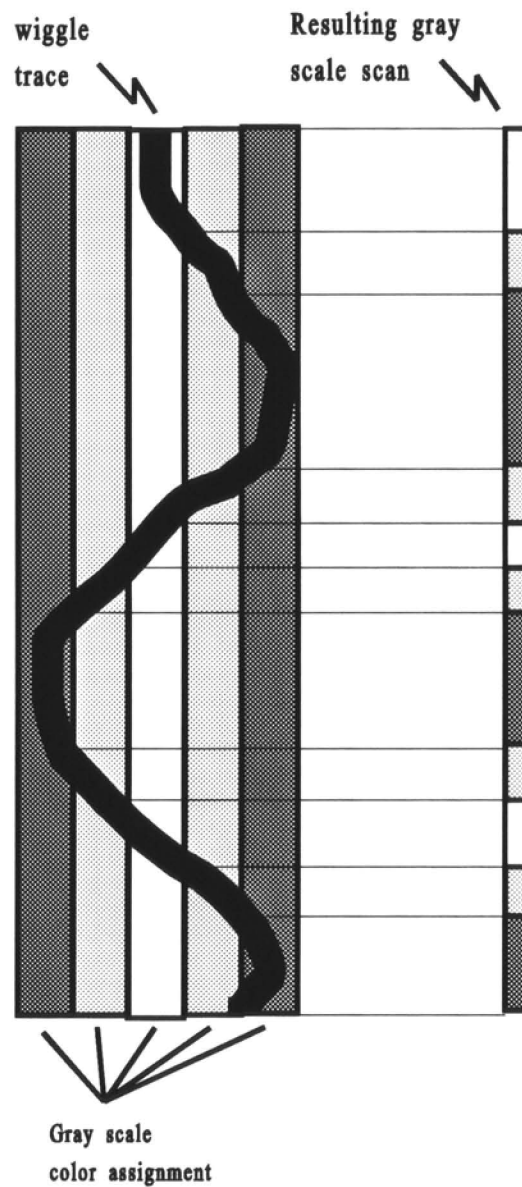
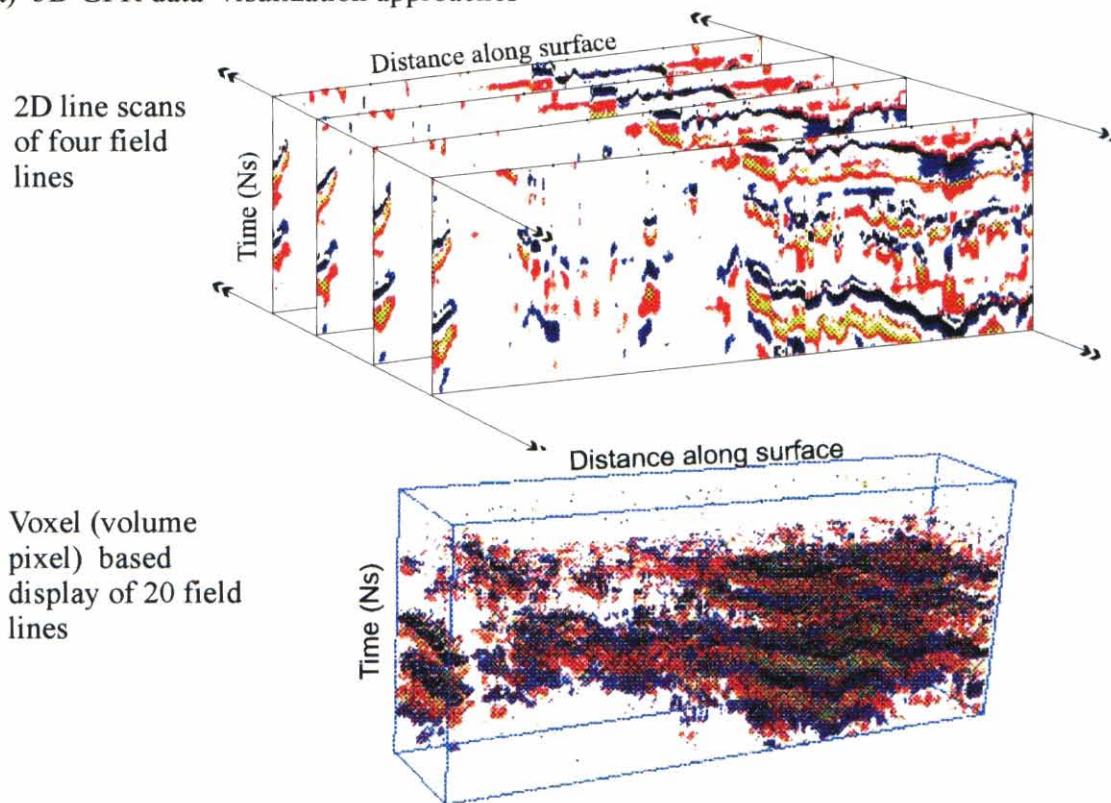


Figure 3. Gray scale (or color) assignment procedures. Gray shades are assigned to different amplitudes on the wiggle trace, producing a gray scale scan. (From Daniels, 1994)

a) 3D GPR data visualization approaches



b) Different ways to slice volume data

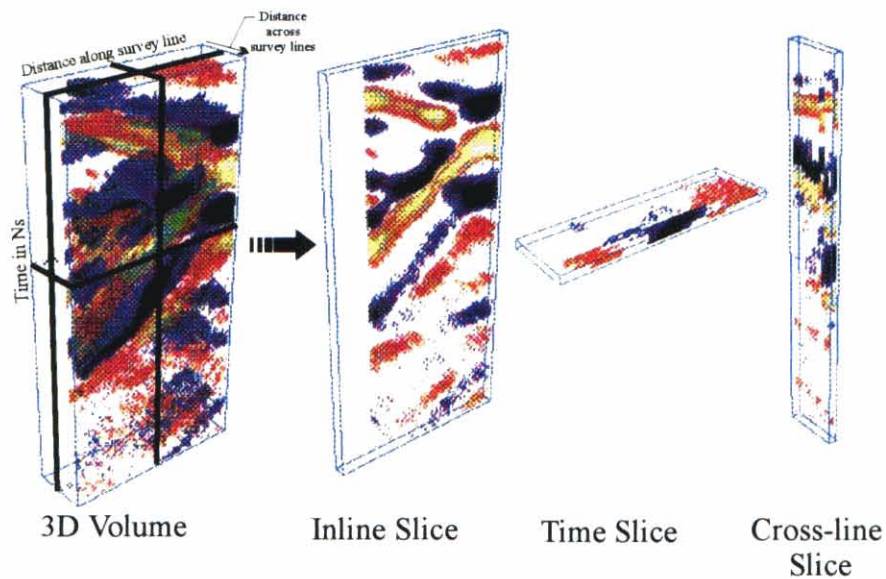


Figure 4. Different 3D volume visualization approaches using GPR data. a) comparison of data visualization using 2D line scan sections versus the voxel based approach with alpha rendering. b) Use of different types of slices of 3D GPR data to help interpretation. (From Daniels et. al. 1997)

polarized, and if it rotates around an axis parallel to the propagation direction it is elliptically polarized (Roberts, 1994). The propagating GPR wave is assumed to be planar, and GPR antennas transmit a linearly polarized field.

There are three facts important to GPR polarization phenomenon: 1) dipole transmit antennas radiate linearly polarized waves, 2) reflections or diffractions from buried targets are often depolarized (this depolarization depends upon the angle of incidence, the impedance contrast, the antenna separation, and the shape and orientation of the target, though the later are not a factor when using a uniform sphere), and 3: dipole receiver antennas are sensitive to the polarization of both reflected and refracted linearly polarized waves (modified from Roberts, 1994)

Section 3: Methods

Measurements were carried out in a large (95"x75"x48"deep) sand box. The sand was moistened before the first set of measurements and the smoothed surface was kept covered with plastic thereafter. Three styrofoam spheres of different sizes (diameters of 2", 6", and 11") were used as targets, uncovered as dielectrics, and wrapped in aluminum foil as conductors. A particular ball size and type was buried, and measurements were carried out with two perpendicular antenna orientations. A GSSI SIR 10 system was used. A wheel was used between the SIR 10 and the bistatic (separate transmitter and receiver) antenna to trigger data sampling from the receiving antenna. The slightest turn of the wheel caused the antenna to send and receive a signal corresponding to one trace, which gave an even distribution of traces along a traverse line. An average of 273 traces per pull was recorded, and data was standardized to this. The data were named and saved on hard disk (see appendix A), on a trace-by-trace basis, with

one traverse line per stored digital file. On one side of the spherical target one line per inch spacing was used in order to achieve good resolution, while the other side was only sampled at a two inch interval between lines because of the symmetry involved. For each set of measurements 34 lines were recorded. The antenna was then realigned, perpendicular to the previous alignment, and the 34 lines were run again. Then the ball was dug out and replaced with another, with meticulous care taken to insure that the target's center did not vary between measurements at the same burial depth. The measurement process was then repeated. Collection of the entire data set was completed over a three week period during February and March of 1998.

Data manipulation was done using a program called RADACAL (developed here at Ohio State by Roger Roberts) and 3-D displays were achieved with a program called BOB. The raw data was byte-swapped, then standardized to 273 traces per line. A one-dimensional filter was then applied to the data, which basically smoothed the traces and removed the DC component of the signal. Two-dimensional images were generated with RADACAL, using a gray scale format. RADACAL essentially lined up traces, and assigned a certain part of the gray scale to each amplitude. See figures 2 and 3. Bright spots and dark spots therefore correspond to high positive or negative amplitudes, which come from the reflectors (or the input wave). The three-dimensional images were generated with BOB. Precise manipulation of the color palette with respect to amplitude was necessary to generate interpretable results. Only one polarity was used for the 3-dimensional images.

Section 4: Results

Effect of ball size:

As was expected, the larger the sphere, the better it showed up on the records (figure 5 and Appendix B). Also, resolution with respect to offset was greater with a larger sphere. There seems to be a limit to the size of a detectable object that depends on the distance to the antenna, and the electrical properties contrast between it and the host medium for a particular frequency of the transmitted signal. This supports numbers 2 and 3 of the aforementioned requirements for detecting a buried object.

Effect of burial depth:

When a wave of electromagnetic radiation is sent into a dielectric half space (moist sand for example) the wavefront begins its traverse closely approximating a hemisphere. It reaches a point, however, at which it is more closely approximated by a plane of radiation. This distinguishes between near field and far field conditions. In the near field modeling of the wave is difficult because of signal interactions with the surface, but the far field is modeled by a plane wave. The two fields reflect data back to the receiver differently. It was hoped that some sign of this would show up on the data, but it does not appear so, though it is believed that the boundary between near and far field was somewhere between one and a half and two feet below the surface.

All the conducting spheres were easy to recognize at both burial depths. They all formed nice parabolic shaped spatial anomaly patterns, although the shapes varied somewhat with ball size (figures 6a, b and c, and Appendix B). The spheres buried at a depth of one foot have the

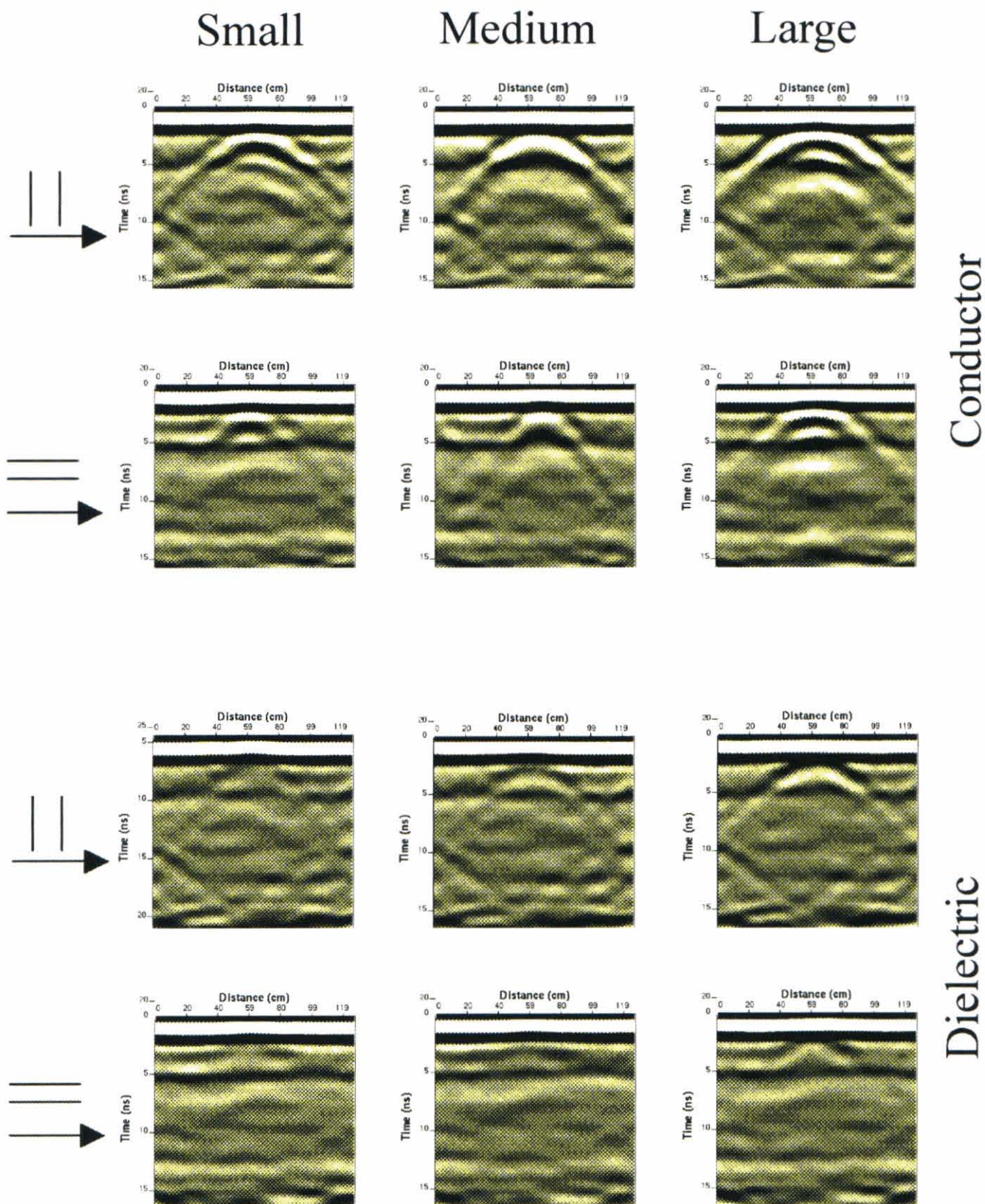


Figure 5a Effect of ball size. Burial depth of 1 foot.
0 offset, for conductors and dielectrics.
With both antenna orientations.

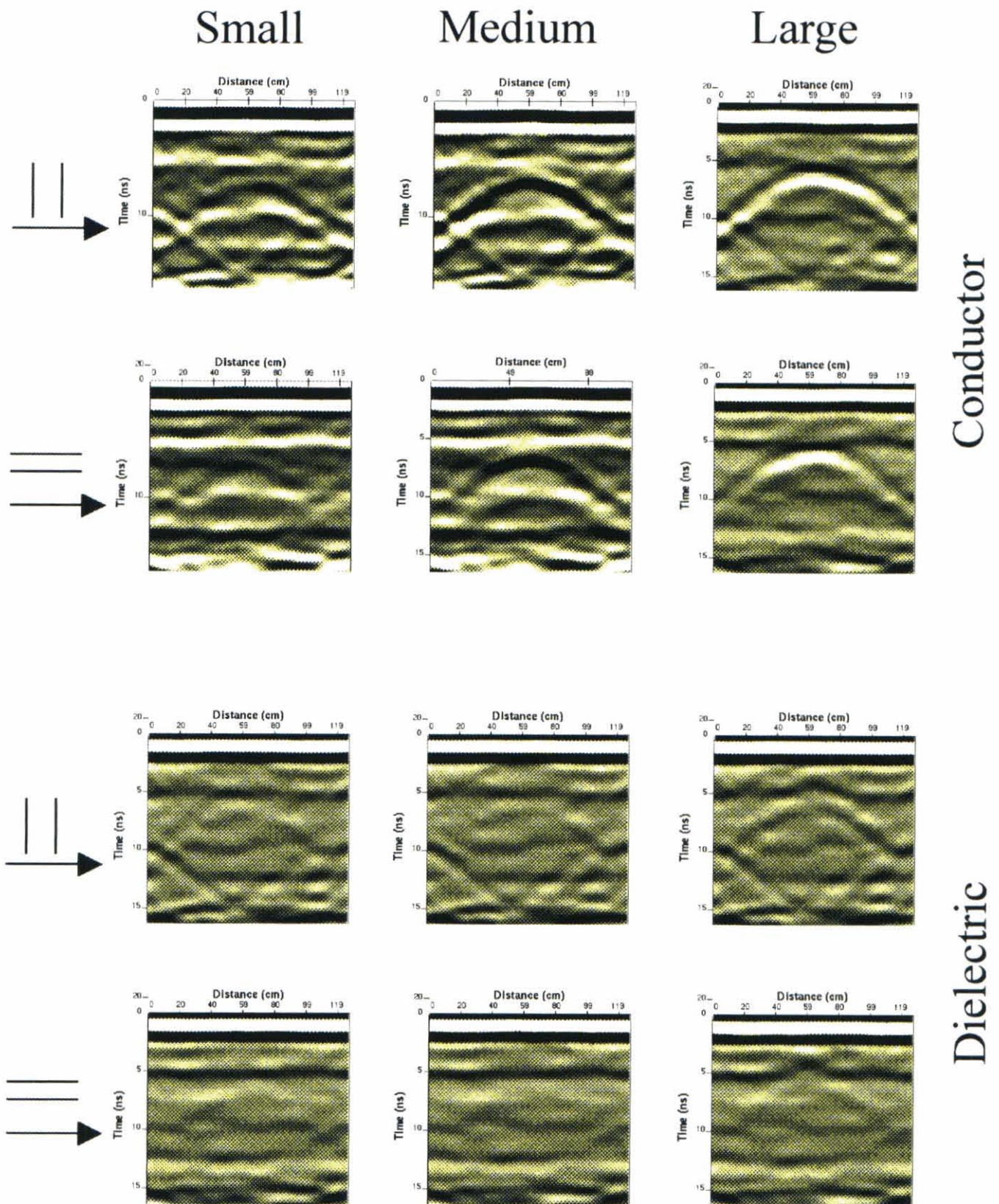


Figure 5b Effect of ball size. Burial depth of 2 feet.
0 offset, for conductors and dielectrics.
With both antenna orientations.

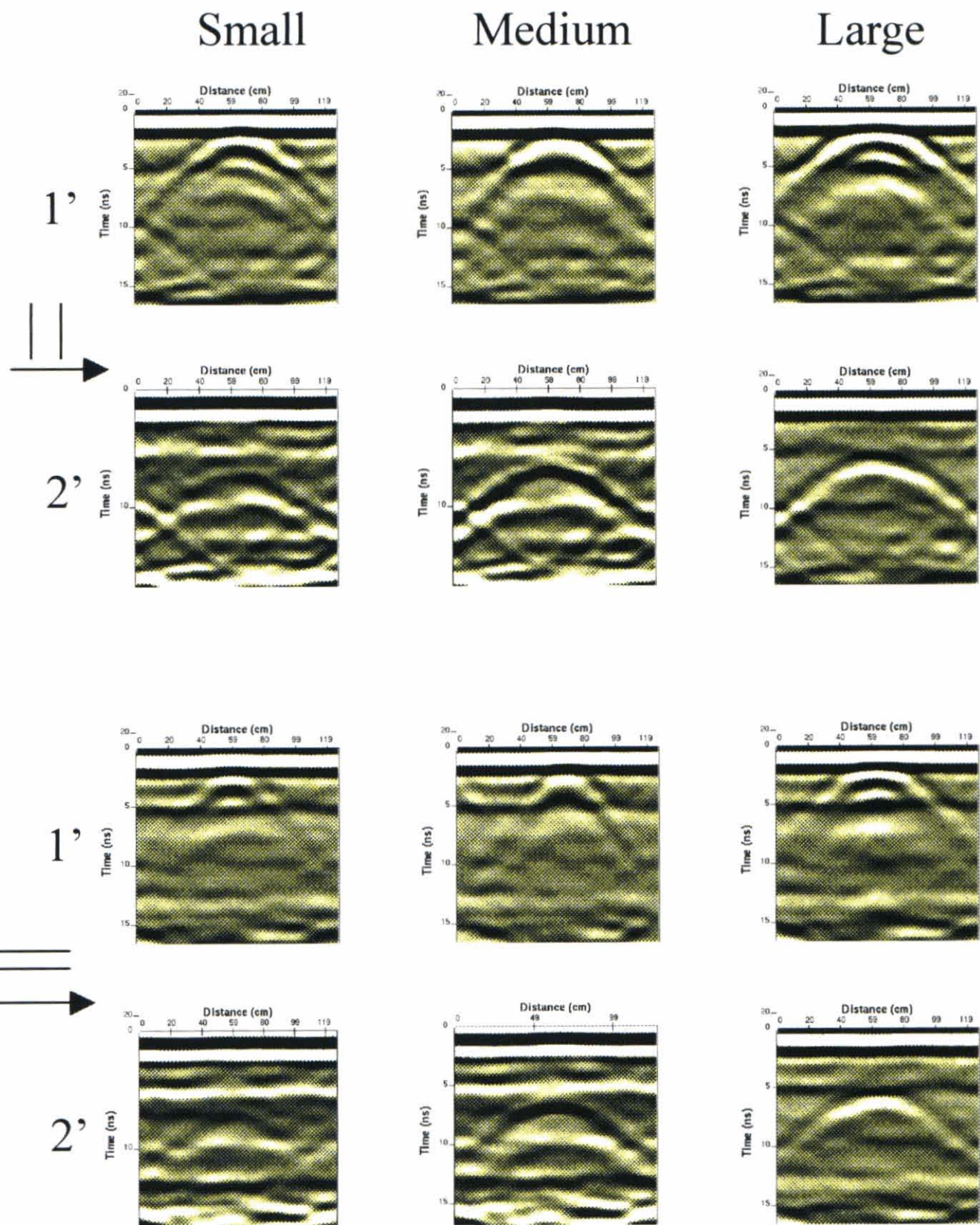


Figure 6a Effect of burial depth. Conductors with 0 offset. Shows both antenna orientations, and all three Ball sizes.

Small

Medium

Large

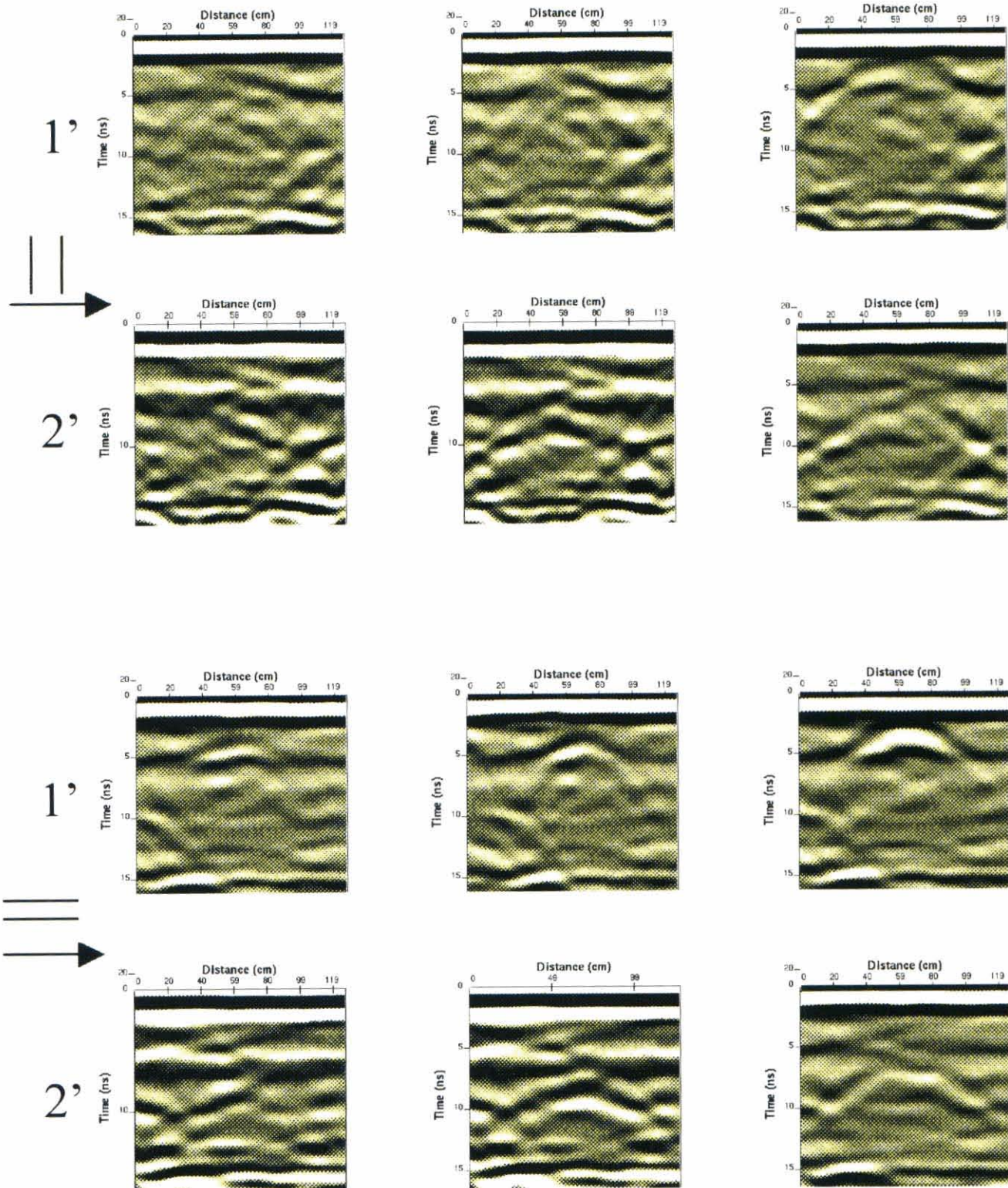


Figure 6b Effect of burial depth. Conductors with 12 inch offset. Shows both antenna orientations, and all three Ball sizes.

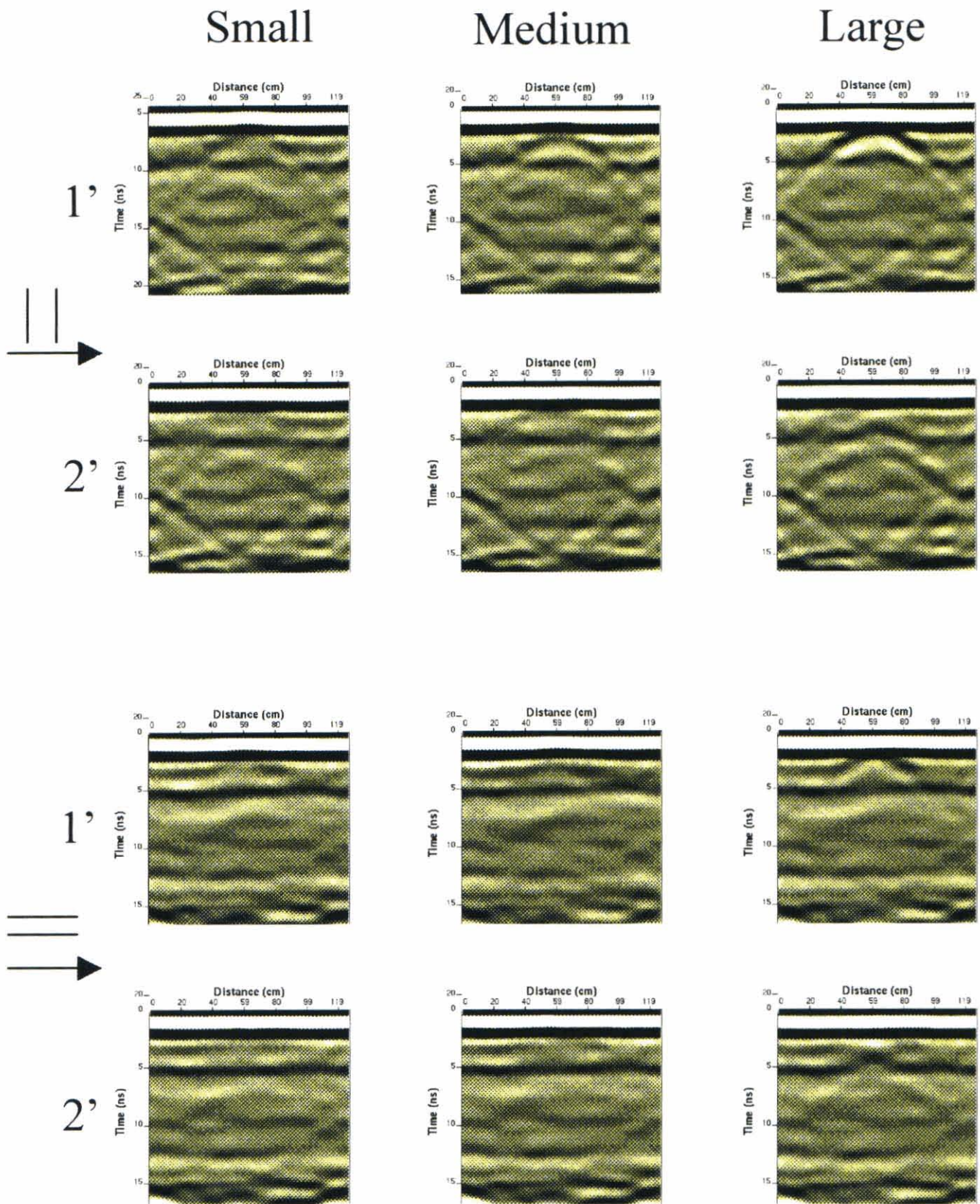


Figure 6c Effect of burial depth. Dielectrics with 0 inch offset. Shows both antenna orientations, and all three Ball sizes.

tops of their reflections masked. This is actually the input signal interfering with the data. This anomaly is present in all of the data as two distinct bands corresponding to high amplitude positive and negative polarities associated with the input wavelet. If something uniform and continuous shows up on GPR data, then it is a good bet that it is not part of the subsurface, but rather some form of outside interference. The dielectric spheres show up at the one foot burial depth, but the small and medium dielectric spheres become hard to recognize at the two foot burial depth. Because such shallow burial depths were used, the input signal has ample strength to reach the targets and propagate back to the antenna. In fact, though masked from a lot of the images, the bottom of the pit shows up quite well on all the data. This satisfies the first requirement for target detection from above.

Effect of ball type:

The aluminum foil covered spheres used were perfect conductors, and the uncovered Styrofoam spheres were a close approximate to perfect dielectrics. Both yielded interpretable results (figure 5 and Appendix B). All the conductors show up well. Some of the records for the deeper dielectrics show little or nothing. Further filtering of the data may have been able to extract clearer images here. The reason the conductors show up so much better than the dielectrics, lies within the size of the electrical properties contrast. At the sand-conductor boundary, which sends back a strong reflection, the contrast in electrical properties is large, while at the sand-dielectric boundary the contrast is not nearly as large, hence the weaker reflection.

Effect of Offset:

Variations in amplitude caused by polarization effects and the antenna pattern were expected in the lines as offset changed, and nulls were expected on some of the lines. The nulls do in fact show up, though more frequently with the antennas oriented parallel to the direction of traverse. The two-way travel time increases as offset is increased, and the positions of the reflectors are moved to a later time on the record (figure 7, and Appendix B). Most of the spheres did not appear on the records all the way out to the maximum offset of 20 inches, and as the lines approach the 20 inch offset, the side of the pit starts to show up on the records.

Effect of Antenna Orientation:

In general, higher amplitude anomalies were achieved with the antennas oriented perpendicular to the direction of traverse than with them parallel. The parabolas are more continuous with this orientation. Nulls were recorded more often on either side of the strong central part of the record with the antennas oriented parallel to the direction of traverse (2cm and 2cmx in Appendix B). Both orientations seem to give results out to the same offset. It is important to note the large differences between the records having identical parameters, but measured with the two different orientations (Appendix B). These differences are due to polarization, and possibly depolarization, at subsurface boundaries. The antenna radiates a plane polarized wave, and the amount of energy that reaches the reflector and is reflected back from the target, and what is actually detected by the receiver depends on the orientation of the antennas with respect to the position of the target.

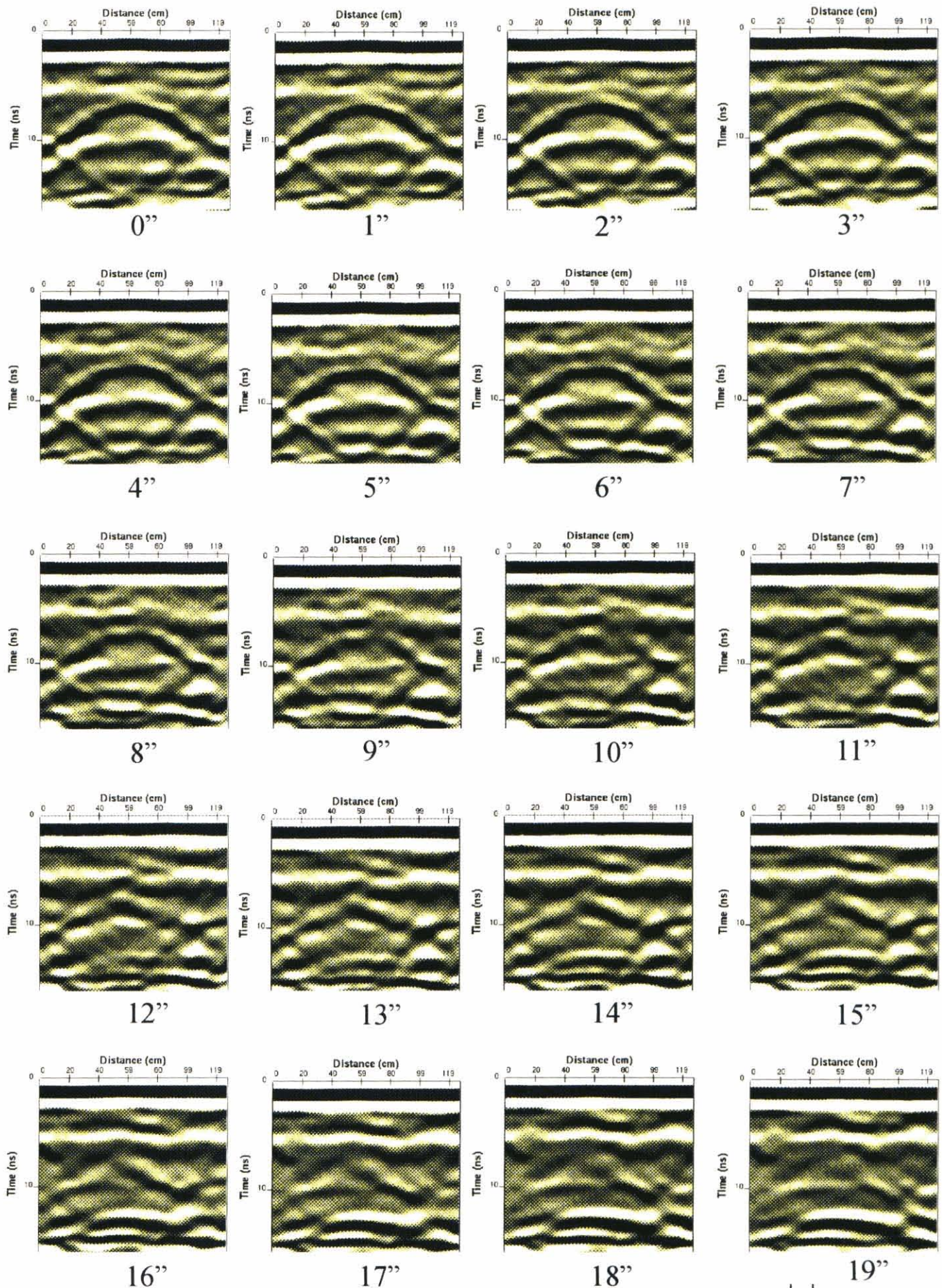


Figure 7a

Effect of offset. Medium conductor buried at 2 feet.



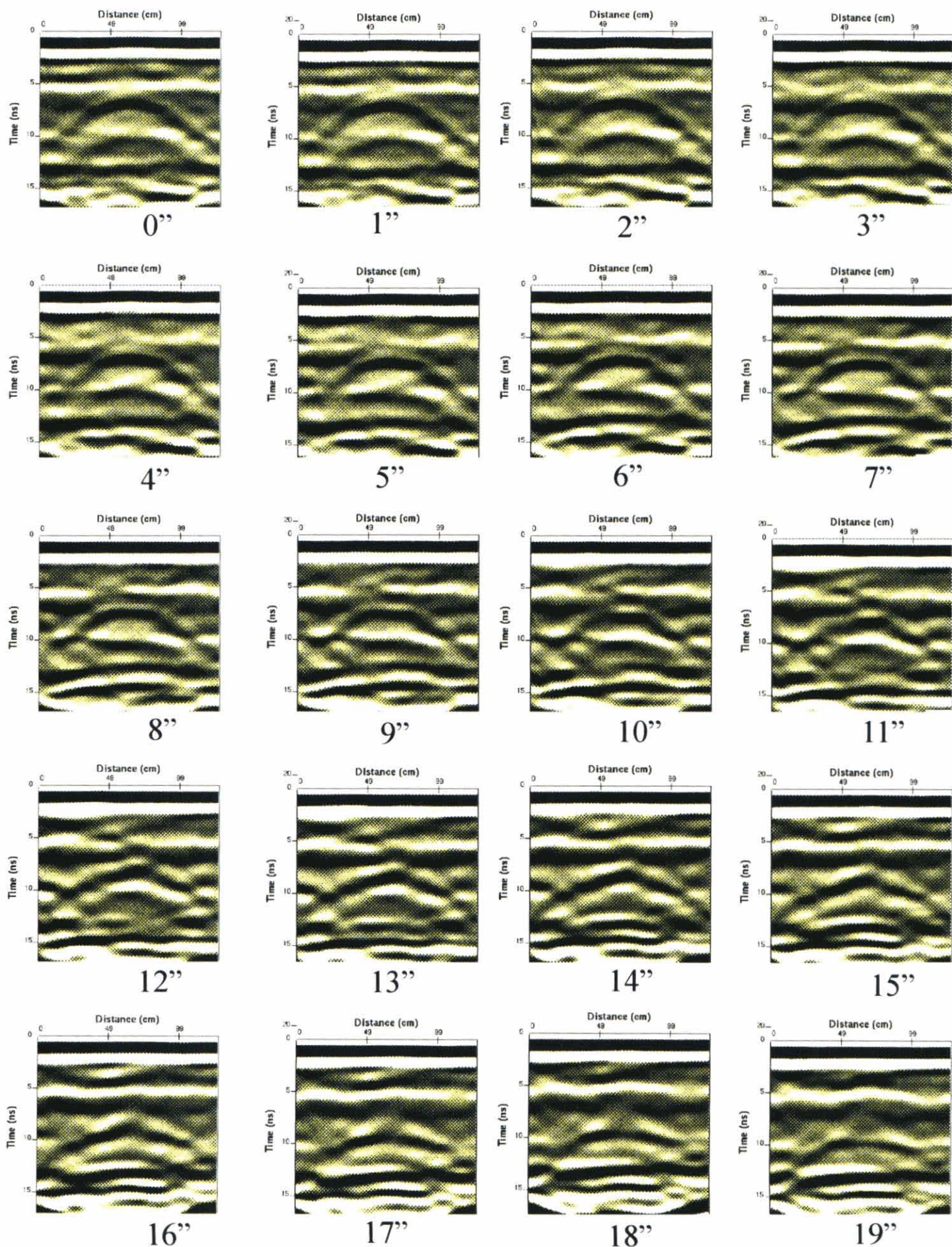
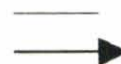


Figure 7b

Effect of offset. Medium conductor buried at 2 feet



3-D Results

Converting the data into interpretable 3-D images required a lot of manipulation. Precise assignment of colors to amplitude ranges was key. Because the 3-D images need to be “transparent”, noise and clutter on several different lines can combine to obscure the target. Further filtering of the data may have aided in the clarity of the 3-D images. Even when the 2-D data was easily interpretable, 3-D images were not always clear. As you can see in the first figure of Appendix C, when the lines are combined properly, a 3-D image can be useful. It can provide more information on the overall size of the target. The nulls caused by effects of polarization that were mentioned earlier can be seen clearly on some of the 3-D images.

Conclusion:

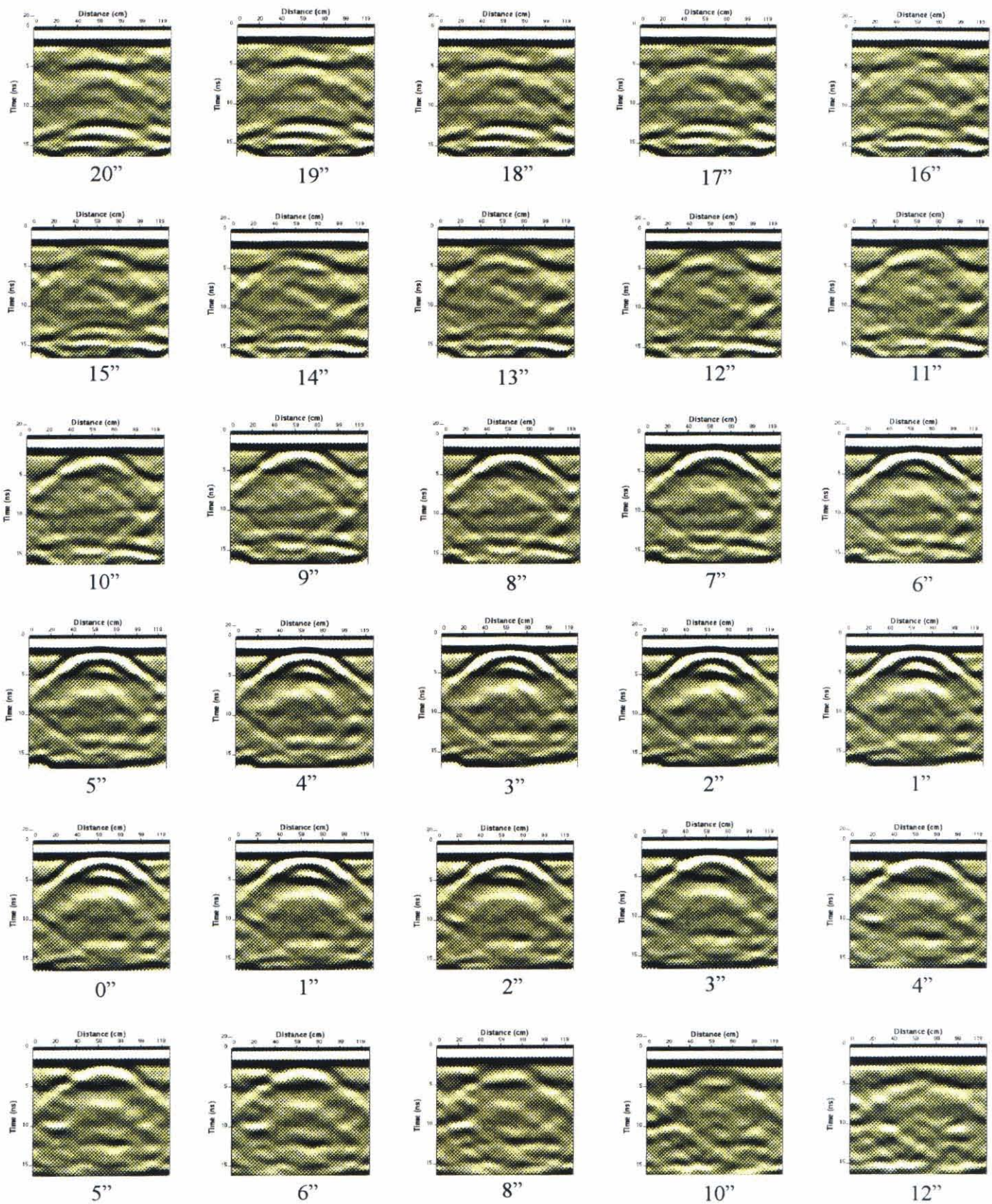
One often thinks of a wave propagating through the subsurface as a uniform hemisphere, and would therefore conclude that the orientation of GPR antennas would make little difference in the resulting data. This is not the case. Because of polarization effects, and the resulting reflected wave pattern, antenna orientation becomes a key factor in identifying and interpreting anomalies associated with subsurface targets in GPR data. The data from this experiment also demonstrates, and follows the requirements for detection of a target, including: 1) the transmitted wave must be strong enough to go to the buried object and return to the surface, 2) the impedance contrast must be high enough, 3) the object must be large enough to be detected at that depth, and 4) Other objects must not interfere.

Line Names

Distance From Center of Antenna to Center of Sphere	small		small		medium		medium		medium		large		large	
	small	small	small	small	medium	medium	medium	medium	medium	medium	large	large	large	large
	conductor at 1 foot	conductor at 1 foot w/ ant. //	conductor at 1 foot w/ ant. //	diallectric at 1 foot w/ ant. //	conductor at 1 foot	conductor at 1 foot w/ ant. //	conductor at 1 foot w/ ant. //	diallectric at 1 foot	diallectric at 1 foot w/ ant. //	conductor at 1 foot	conductor at 1 foot w/ ant. //	conductor at 1 foot w/ ant. //	diallectric at 1 foot	diallectric at 1 foot w/ ant. //
-20	1cs70	1csx70	1ds70	1dsx70	1cm70	1cmx70	1dm70	1dmx70	1el70	1elx70	1el70	1elx70	1dl70	1dlx70
-18	1cs68	1csx68	1ds68	1dsx68	1cm68	1cmx68	1dm68	1dmx68	1el68	1elx68	1el68	1elx68	1dl68	1dlx68
-16	1cs66	1csx66	1ds66	1dsx66	1cm66	1cmx66	1dm66	1dmx66	1el66	1elx66	1el66	1elx66	1dl66	1dlx66
-14	1cs64	1csx64	1ds64	1dsx64	1cm64	1cmx64	1dm64	1dmx64	1el64	1elx64	1el64	1elx64	1dl64	1dlx64
-12	1cs62	1csx62	1ds62	1dsx62	1cm62	1cmx62	1dm62	1dmx62	1el62	1elx62	1el62	1elx62	1dl62	1dlx62
-10	1cs60	1csx60	1ds60	1dsx60	1cm60	1cmx60	1dm60	1dmx60	1el60	1elx60	1el60	1elx60	1dl60	1dlx60
-8	1cs58	1csx58	1ds58	1dsx58	1cm58	1cmx58	1dm58	1dmx58	1el58	1elx58	1el58	1elx58	1dl58	1dlx58
-6	1cs56	1csx56	1ds56	1dsx56	1cm56	1cmx56	1dm56	1dmx56	1el56	1elx56	1el56	1elx56	1dl56	1dlx56
-5	1cs55	1csx55	1ds55	1dsx55	1cm55	1cmx55	1dm55	1dmx55	1el55	1elx55	1el55	1elx55	1dl55	1dlx55
-4	1cs54	1csx54	1ds54	1dsx54	1cm54	1cmx54	1dm54	1dmx54	1el54	1elx54	1el54	1elx54	1dl54	1dlx54
-3	1cs53	1csx53	1ds53	1dsx53	1cm53	1cmx53	1dm53	1dmx53	1el53	1elx53	1el53	1elx53	1dl53	1dlx53
-2	1cs52	1csx52	1ds52	1dsx52	1cm52	1cmx52	1dm52	1dmx52	1el52	1elx52	1el52	1elx52	1dl52	1dlx52
-1	1cs51	1csx51	1ds51	1dsx51	1cm51	1cmx51	1dm51	1dmx51	1el51	1elx51	1el51	1elx51	1dl51	1dlx51
0	1cs50	1csx50	1ds50	1dsx50	1cm50	1cmx50	1dm50	1dmx50	1el50	1elx50	1el50	1elx50	1dl50	1dlx50
1	1cs49	1csx49	1ds49	1dsx49	1cm49	1cmx49	1dm49	1dmx49	1el49	1elx49	1el49	1elx49	1dl49	1dlx49
2	1cs48	1csx48	1ds48	1dsx48	1cm48	1cmx48	1dm48	1dmx48	1el48	1elx48	1el48	1elx48	1dl48	1dlx48
3	1cs47	1csx47	1ds47	1dsx47	1cm47	1cmx47	1dm47	1dmx47	1el47	1elx47	1el47	1elx47	1dl47	1dlx47
4	1cs46	1csx46	1ds46	1dsx46	1cm46	1cmx46	1dm46	1dmx46	1el46	1elx46	1el46	1elx46	1dl46	1dlx46
5	1cs45	1csx45	1ds45	1dsx45	1cm45	1cmx45	1dm45	1dmx45	1el45	1elx45	1el45	1elx45	1dl45	1dlx45
6	1cs44	1csx44	1ds44	1dsx44	1cm44	1cmx44	1dm44	1dmx44	1el44	1elx44	1el44	1elx44	1dl44	1dlx44
7	1cs43	1csx43	1ds43	1dsx43	1cm43	1cmx43	1dm43	1dmx43	1el43	1elx43	1el43	1elx43	1dl43	1dlx43
8	1cs42	1csx42	1ds42	1dsx42	1cm42	1cmx42	1dm42	1dmx42	1el42	1elx42	1el42	1elx42	1dl42	1dlx42
9	1cs41	1csx41	1ds41	1dsx41	1cm41	1cmx41	1dm41	1dmx41	1el41	1elx41	1el41	1elx41	1dl41	1dlx41
10	1cs40	1csx40	1ds40	1dsx40	1cm40	1cmx40	1dm40	1dmx40	1el40	1elx40	1el40	1elx40	1dl40	1dlx40
11	1cs39	1csx39	1ds39	1dsx39	1cm39	1cmx39	1dm39	1dmx39	1el39	1elx39	1el39	1elx39	1dl39	1dlx39
12	1cs38	1csx38	1ds38	1dsx38	1cm38	1cmx38	1dm38	1dmx38	1el38	1elx38	1el38	1elx38	1dl38	1dlx38
13	1cs37	1csx37	1ds37	1dsx37	1cm37	1cmx37	1dm37	1dmx37	1el37	1elx37	1el37	1elx37	1dl37	1dlx37
14	1cs36	1csx36	1ds36	1dsx36	1cm36	1cmx36	1dm36	1dmx36	1el36	1elx36	1el36	1elx36	1dl36	1dlx36
15	1cs35	1csx35	1ds35	1dsx35	1cm35	1cmx35	1dm35	1dmx35	1el35	1elx35	1el35	1elx35	1dl35	1dlx35
16	1cs34	1csx34	1ds34	1dsx34	1cm34	1cmx34	1dm34	1dmx34	1el34	1elx34	1el34	1elx34	1dl34	1dlx34
17	1cs33	1csx33	1ds33	1dsx33	1cm33	1cmx33	1dm33	1dmx33	1el33	1elx33	1el33	1elx33	1dl33	1dlx33
18	1cs32	1csx32	1ds32	1dsx32	1cm32	1cmx32	1dm32	1dmx32	1el32	1elx32	1el32	1elx32	1dl32	1dlx32
19	1cs31	1csx31	1ds31	1dsx31	1cm31	1cmx31	1dm31	1dmx31	1el31	1elx31	1el31	1elx31	1dl31	1dlx31
20	1cs30	1csx30	1ds30	1dsx30	1cm30	1cmx30	1dm30	1dmx30	1el30	1elx30	1el30	1elx30	1dl30	1dlx30

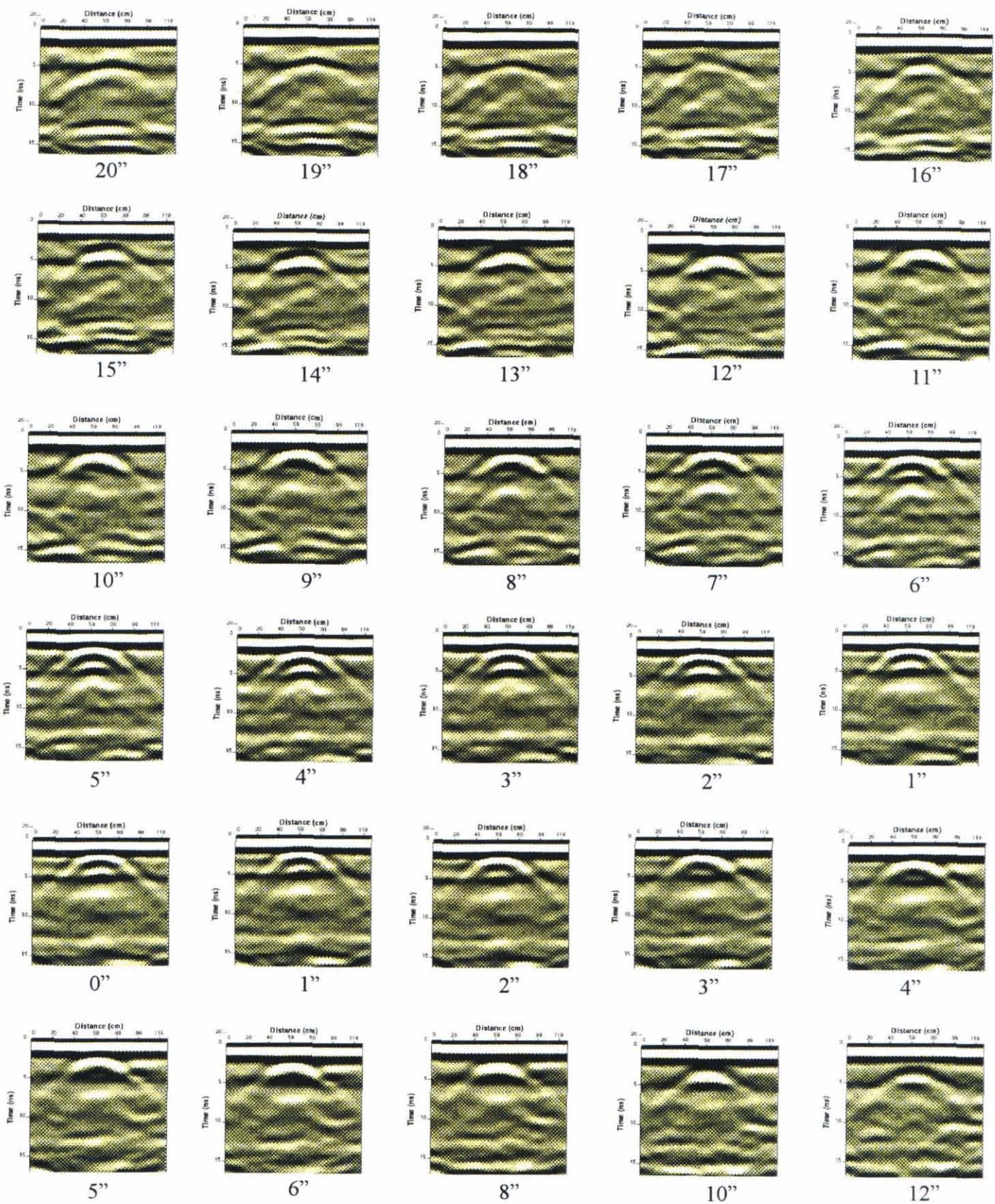
Line Names

Distance From Center of Antenna to Center of Sphere	small		small		medium		medium		medium		large		large	
	conductor		dialectric at		conductor		dialectric at		conductor		conductor		dialectric at	
	at 2 feet	ant. //	2 feet	ant. //	at 2 feet	ant. //	2 feet	ant. //	at 2 feet	ant. //	at 2 feet	ant. //	2 feet	ant. //
-20	2cs70	2csx70	2ds70	2dsx70	2cm70	2cmx70	2dm70	2dmx70	2cl70	2clx70	2cl70	2clx70	2dl70	2dlx70
-18	2cs68	2csx68	2ds68	2dsx68	2cm68	2cmx68	2dm68	2dmx68	2cl68	2clx68	2cl68	2clx68	2dl68	2dlx68
-16	2cs66	2csx66	2ds66	2dsx66	2cm66	2cmx66	2dm66	2dmx66	2cl66	2clx66	2cl66	2clx66	2dl66	2dlx66
-14	2cs64	2csx64	2ds64	2dsx64	2cm64	2cmx64	2dm64	2dmx64	2cl64	2clx64	2cl64	2clx64	2dl64	2dlx64
-12	2cs62	2csx62	2ds62	2dsx62	2cm62	2cmx62	2dm62	2dmx62	2cl62	2clx62	2cl62	2clx62	2dl62	2dlx62
-10	2cs60	2csx60	2ds60	2dsx60	2cm60	2cmx60	2dm60	2dmx60	2cl60	2clx60	2cl60	2clx60	2dl60	2dlx60
-8	2cs58	2csx58	2ds58	2dsx58	2cm58	2cmx58	2dm58	2dmx58	2cl58	2clx58	2cl58	2clx58	2dl58	2dlx58
-6	2cs56	2csx56	2ds56	2dsx56	2cm56	2cmx56	2dm56	2dmx56	2cl56	2clx56	2cl56	2clx56	2dl56	2dlx56
-5	2cs55	2csx55	2ds55	2dsx55	2cm55	2cmx55	2dm55	2dmx55	2cl55	2clx55	2cl55	2clx55	2dl55	2dlx55
-4	2cs54	2csx54	2ds54	2dsx54	2cm54	2cmx54	2dm54	2dmx54	2cl54	2clx54	2cl54	2clx54	2dl54	2dlx54
-3	2cs53	2csx53	2ds53	2dsx53	2cm53	2cmx53	2dm53	2dmx53	2cl53	2clx53	2cl53	2clx53	2dl53	2dlx53
-2	2cs52	2csx52	2ds52	2dsx52	2cm52	2cmx52	2dm52	2dmx52	2cl52	2clx52	2cl52	2clx52	2dl52	2dlx52
-1	2cs51	2csx51	2ds51	2dsx51	2cm51	2cmx51	2dm51	2dmx51	2cl51	2clx51	2cl51	2clx51	2dl51	2dlx51
0	2cs50	2csx50	2ds50	2dsx50	2cm50	2cmx50	2dm50	2dmx50	2cl50	2clx50	2cl50	2clx50	2dl50	2dlx50
1	2cs49	2csx49	2ds49	2dsx49	2cm49	2cmx49	2dm49	2dmx49	2cl49	2clx49	2cl49	2clx49	2dl49	2dlx49
2	2cs48	2csx48	2ds48	2dsx48	2cm48	2cmx48	2dm48	2dmx48	2cl48	2clx48	2cl48	2clx48	2dl48	2dlx48
3	2cs47	2csx47	2ds47	2dsx47	2cm47	2cmx47	2dm47	2dmx47	2cl47	2clx47	2cl47	2clx47	2dl47	2dlx47
4	2cs46	2csx46	2ds46	2dsx46	2cm46	2cmx46	2dm46	2dmx46	2cl46	2clx46	2cl46	2clx46	2dl46	2dlx46
5	2cs45	2csx45	2ds45	2dsx45	2cm45	2cmx45	2dm45	2dmx45	2cl45	2clx45	2cl45	2clx45	2dl45	2dlx45
6	2cs44	2csx44	2ds44	2dsx44	2cm44	2cmx44	2dm44	2dmx44	2cl44	2clx44	2cl44	2clx44	2dl44	2dlx44
7	2cs43	2csx43	2ds43	2dsx43	2cm43	2cmx43	2dm43	2dmx43	2cl43	2clx43	2cl43	2clx43	2dl43	2dlx43
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9	2cs41	2csx41	2ds41	2dsx41	2cm41	2cmx41	2dm41	2dmx41	2cl41	2clx41	2cl41	2clx41	2dl41	2dlx41
10	2cs40	2csx40	2ds40	2dsx40	2cm40	2cmx40	2dm40	2dmx40	2cl40	2clx40	2cl40	2clx40	2dl40	2dlx40
11	2cs39	2csx39	2ds39	2dsx39	2cm39	2cmx39	2dm39	2dmx39	2cl39	2clx39	2cl39	2clx39	2dl39	2dlx39
12	2cs38	2csx38	2ds38	2dsx38	2cm38	2cmx38	2dm38	2dmx38	2cl38	2clx38	2cl38	2clx38	2dl38	2dlx38
13	2cs37	2csx37	2ds37	2dsx37	2cm37	2cmx37	2dm37	2dmx37	2cl37	2clx37	2cl37	2clx37	2dl37	2dlx37
14	2cs36	2csx36	2ds36	2dsx36	2cm36	2cmx36	2dm36	2dmx36	2cl36	2clx36	2cl36	2clx36	2dl36	2dlx36
15	2cs35	2csx35	2ds35	2dsx35	2cm35	2cmx35	2dm35	2dmx35	2cl35	2clx35	2cl35	2clx35	2dl35	2dlx35
16	2cs34	2csx34	2ds34	2dsx34	2cm34	2cmx34	2dm34	2dmx34	2cl34	2clx34	2cl34	2clx34	2dl34	2dlx34
17	2cs33	2csx33	2ds33	2dsx33	2cm33	2cmx33	2dm33	2dmx33	2cl33	2clx33	2cl33	2clx33	2dl33	2dlx33
18	2cs32	2csx32	2ds32	2dsx32	2cm32	2cmx32	2dm32	2dmx32	2cl32	2clx32	2cl32	2clx32	2dl32	2dlx32
19	2cs31	2csx31	2ds31	2dsx31	2cm31	2cmx31	2dm31	2dmx31	2cl31	2clx31	2cl31	2clx31	2dl31	2dlx31
20	2cs30	2csx30	2ds30	2dsx30	2cm30	2cmx30	2dm30	2dmx30	2cl30	2clx30	2cl30	2clx30	2dl30	2dlx30



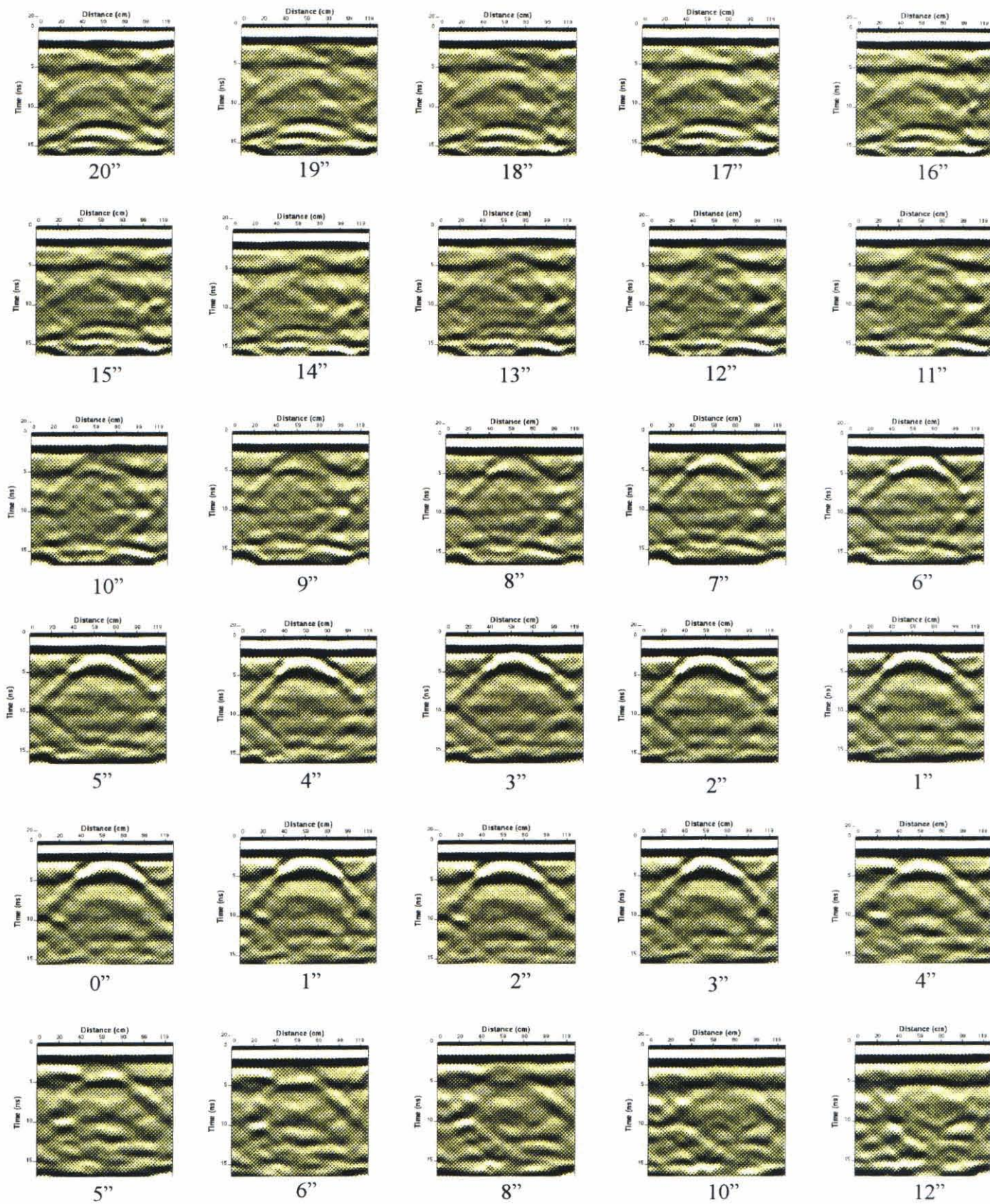
1cl: large conductor at 1 foot





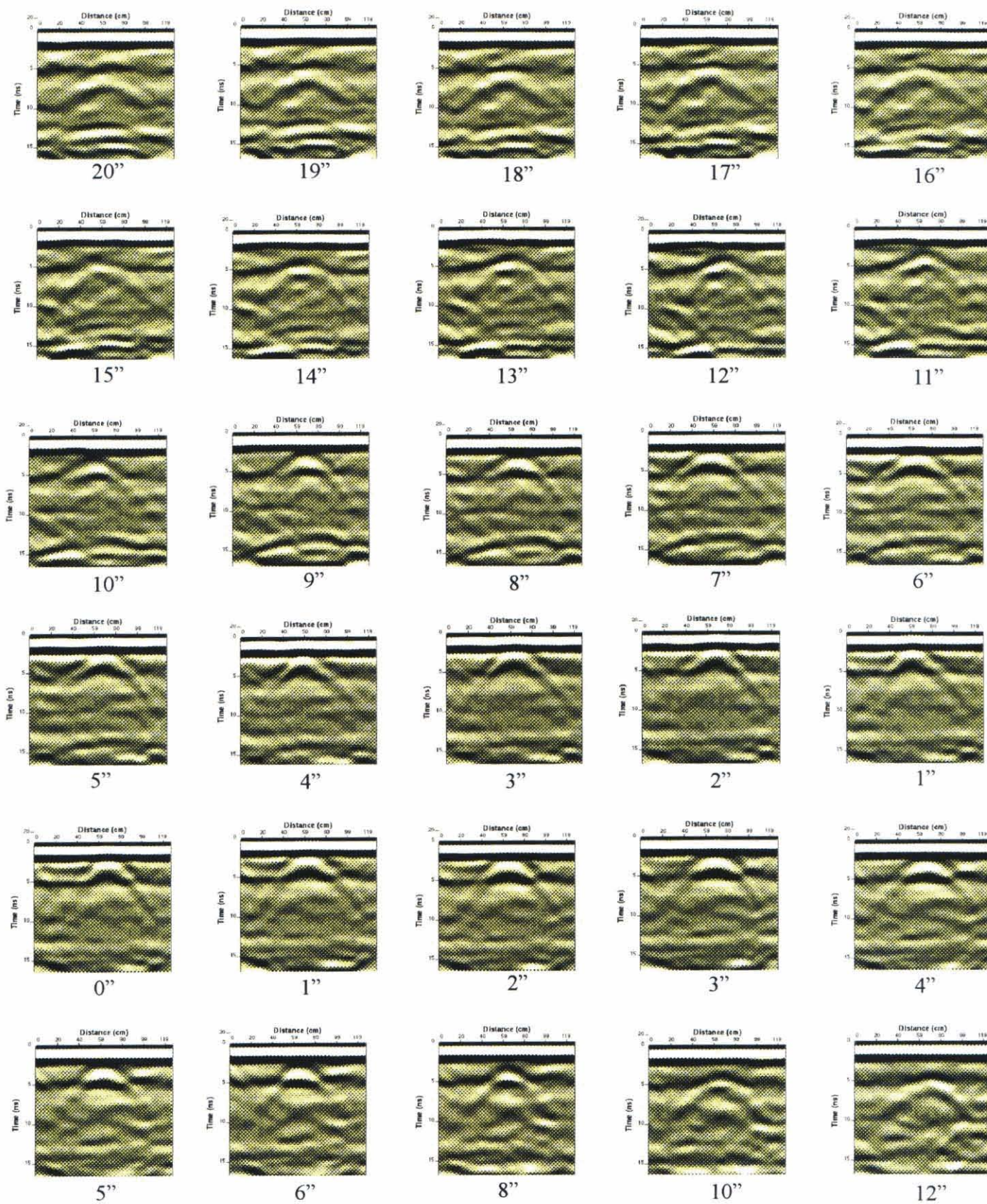
1clx: large conductor at 1 foot





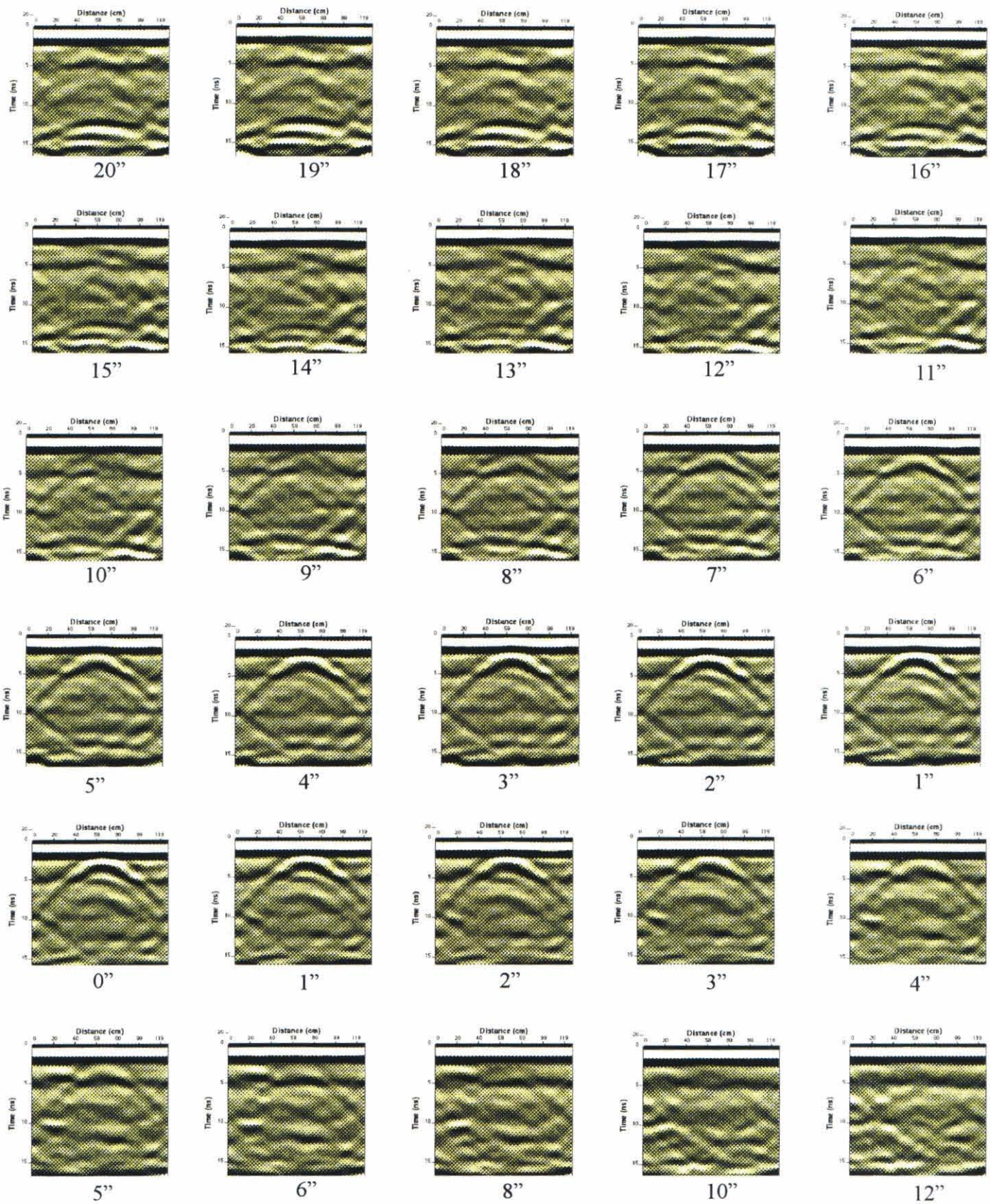
1cm: medium conductor at 1 foot





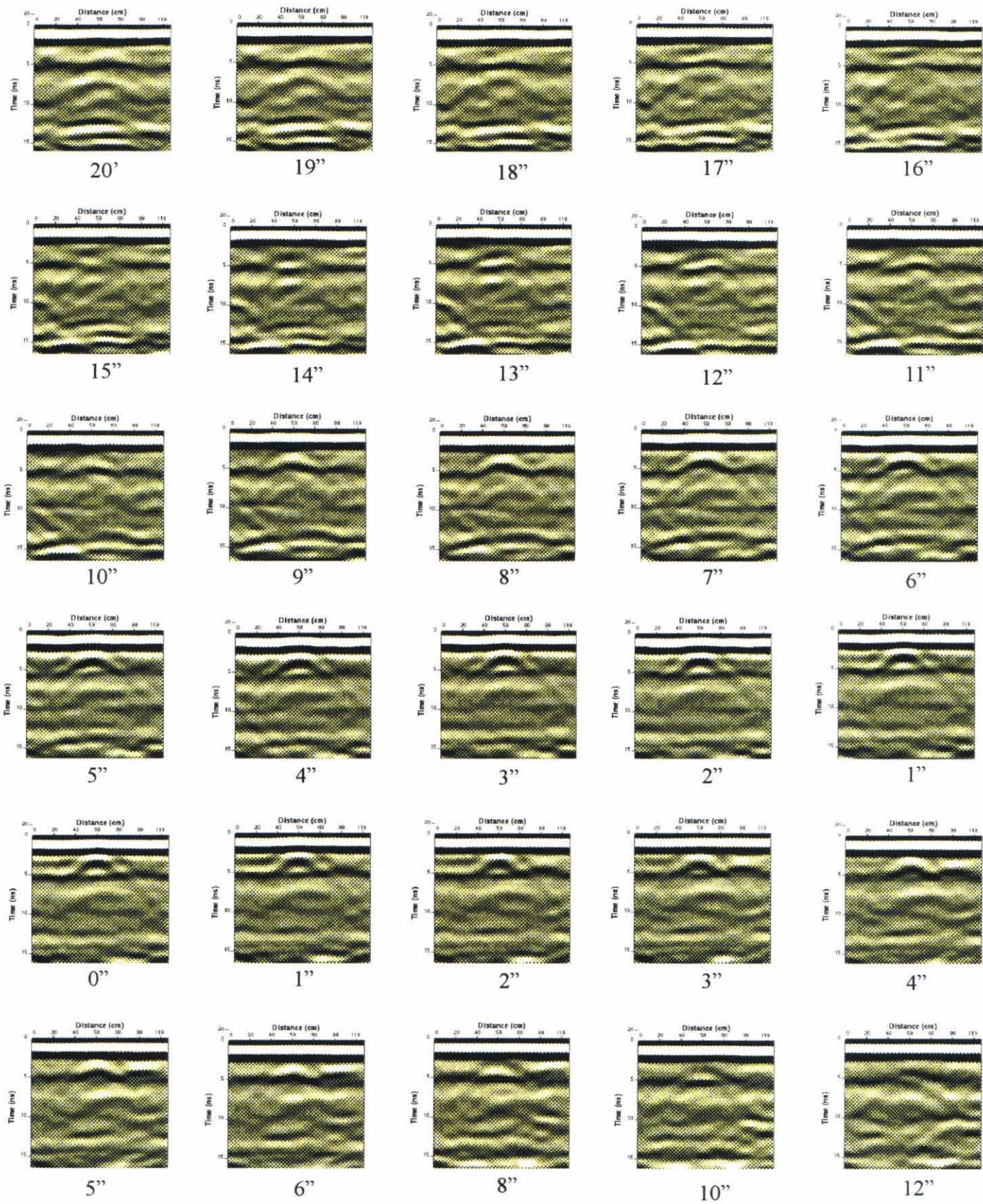
1cmx: medium conductor at 1 foot





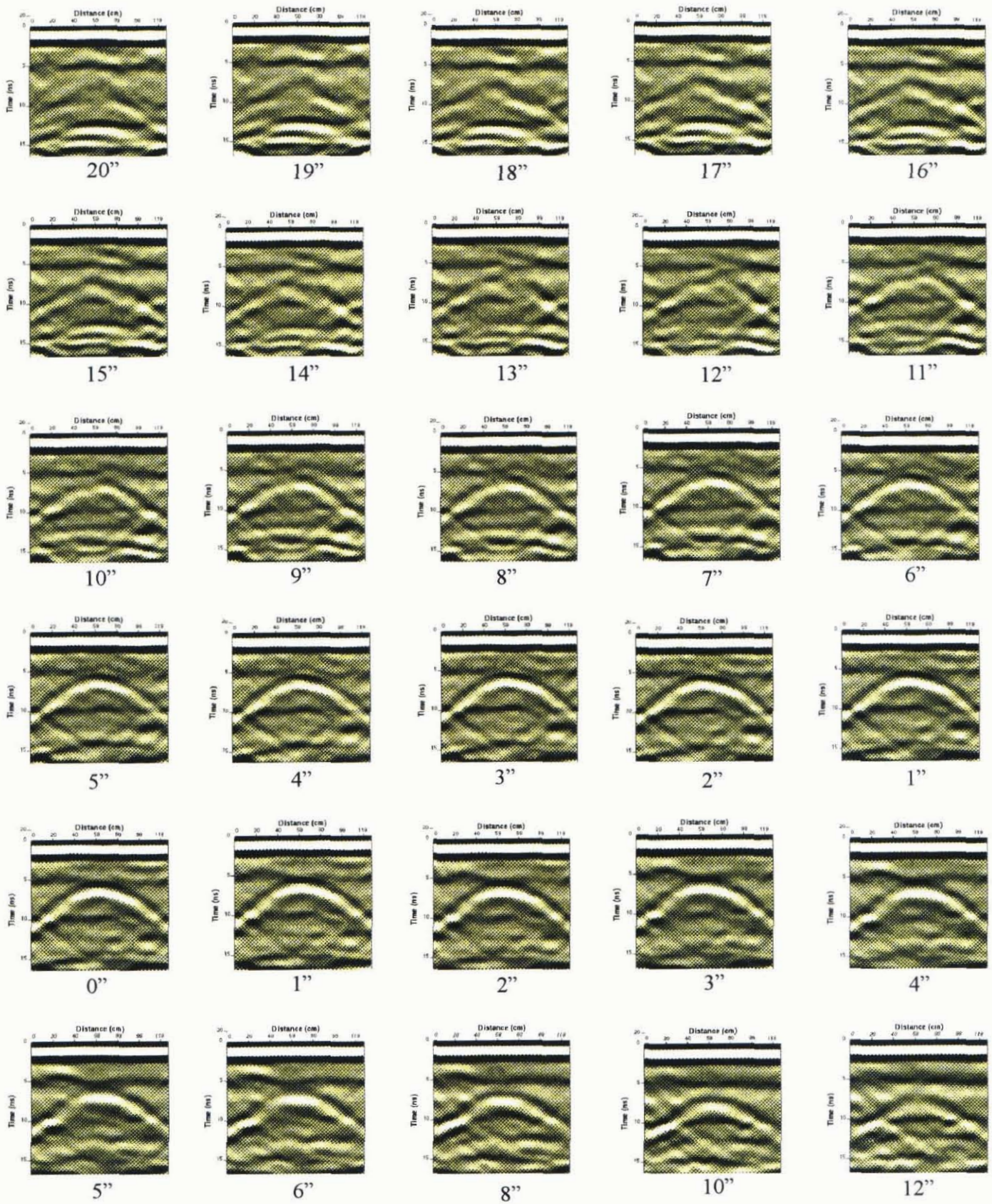
1cs: small conductor at 1 foot





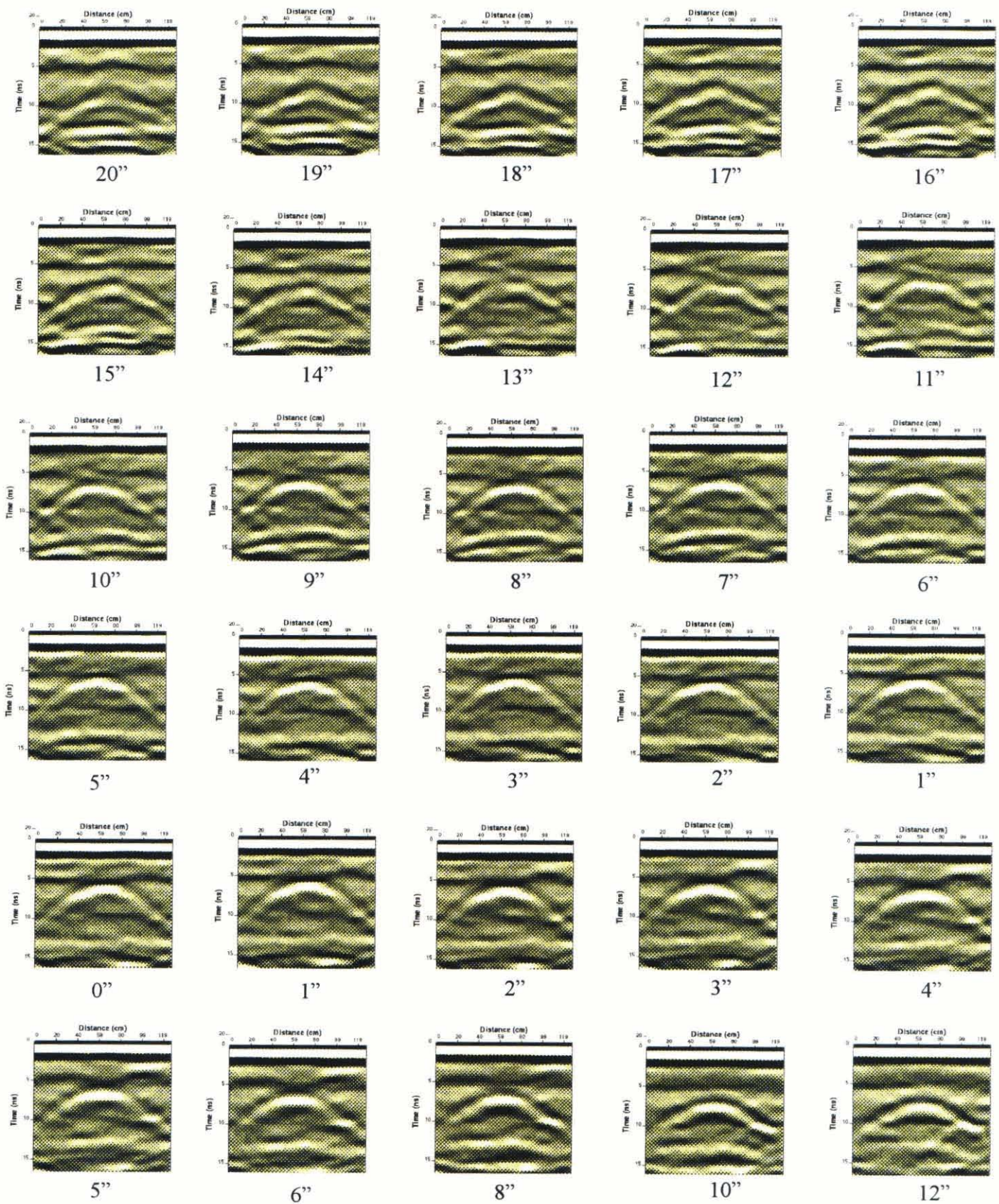
1csx: small conductor at 1 foot





2cl: large conductor at 2 feet





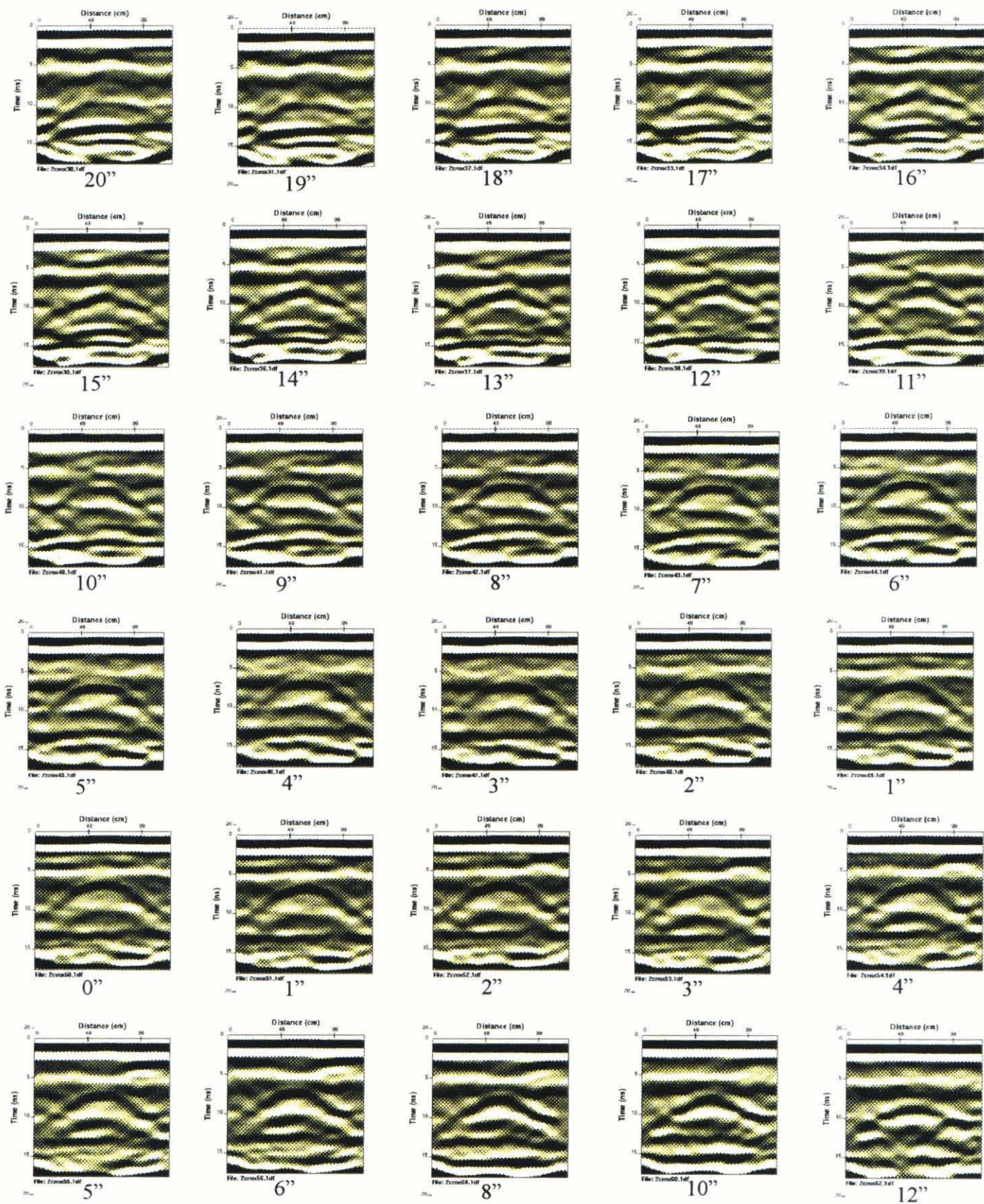
2clx: large conductor at 2 feet





2cm: medium conductor at 2 feet





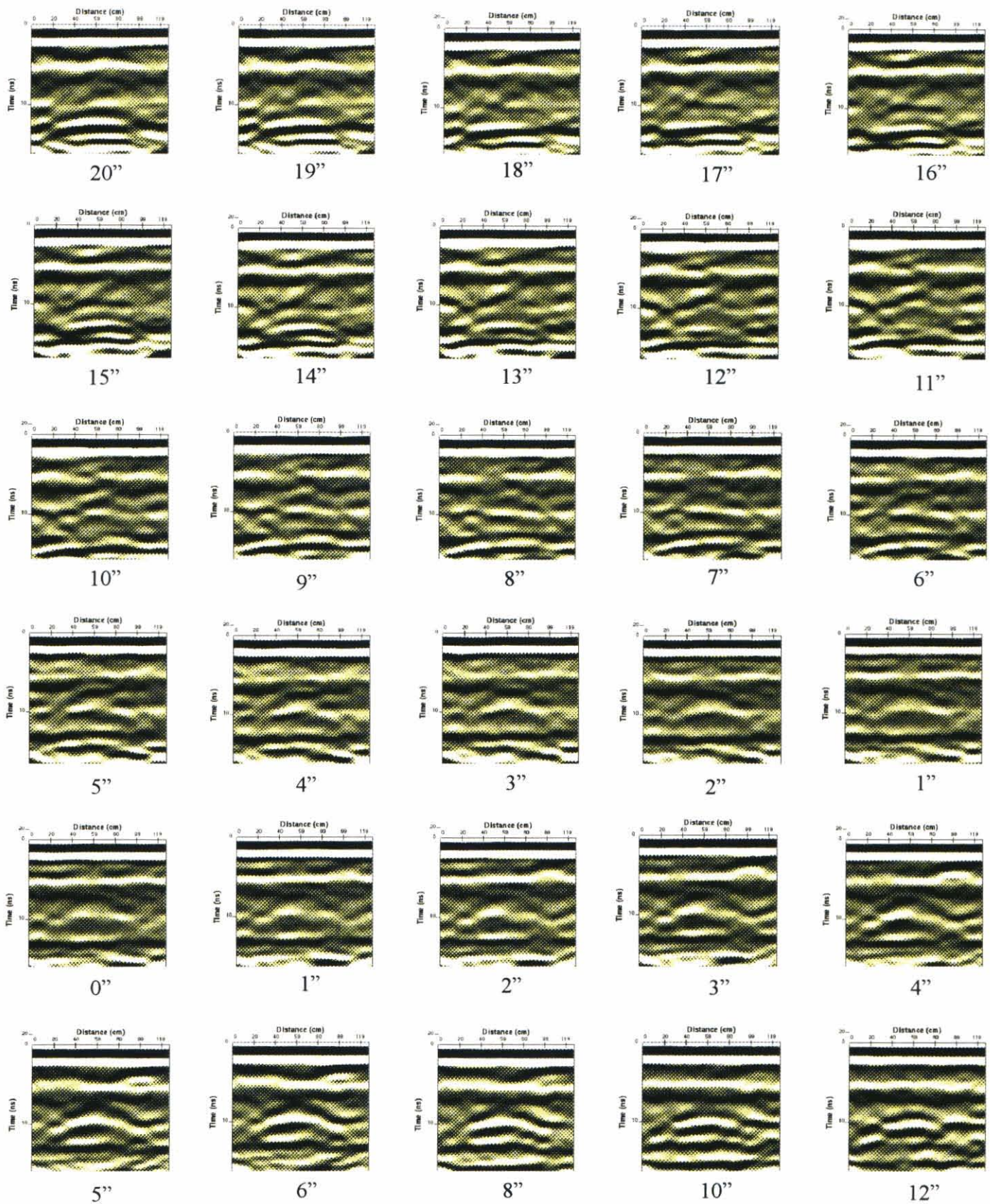
2cmx: medium conductor at 2 feet





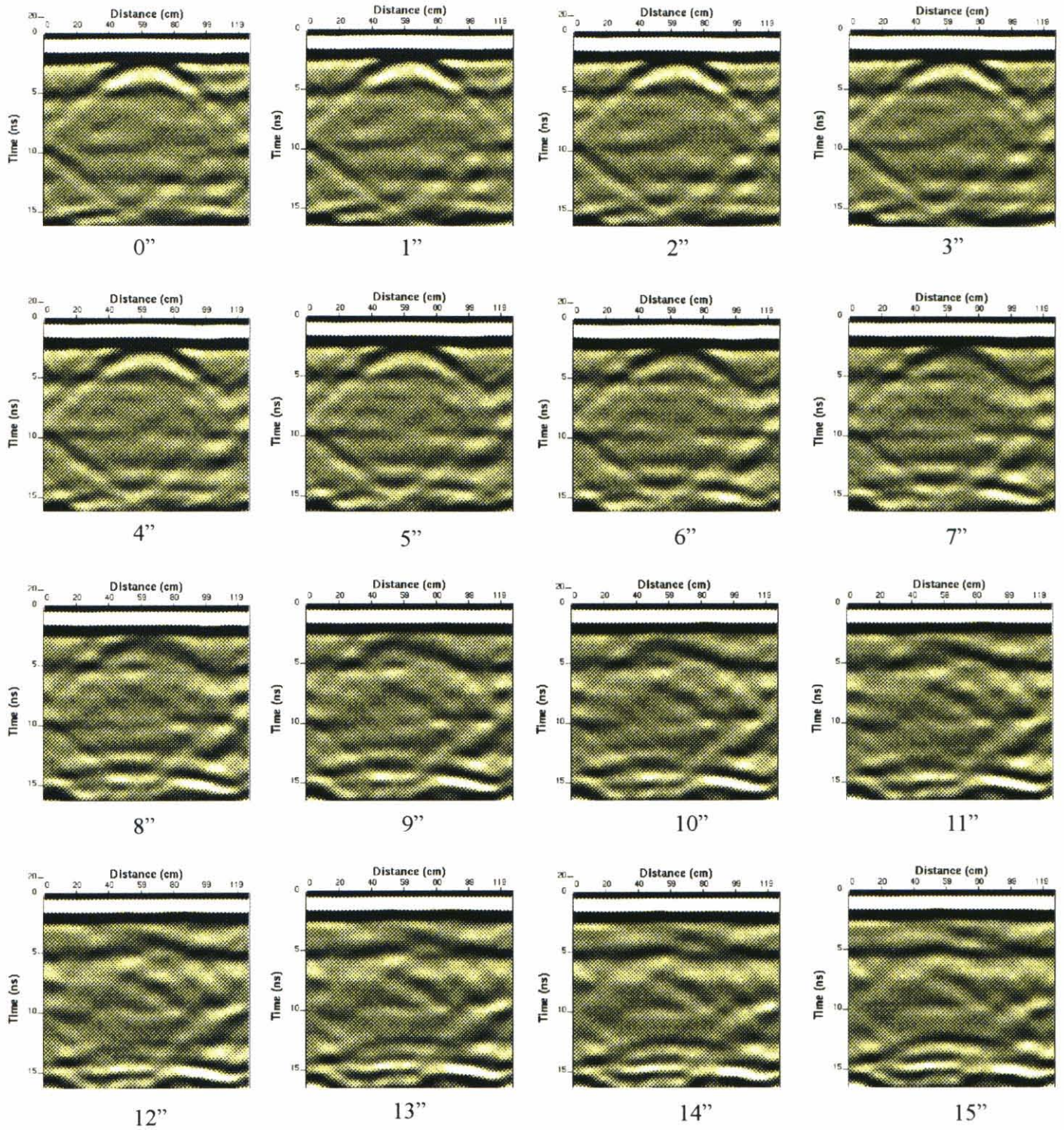
2cs: small conductor buried at 2 feet.



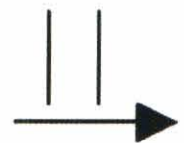


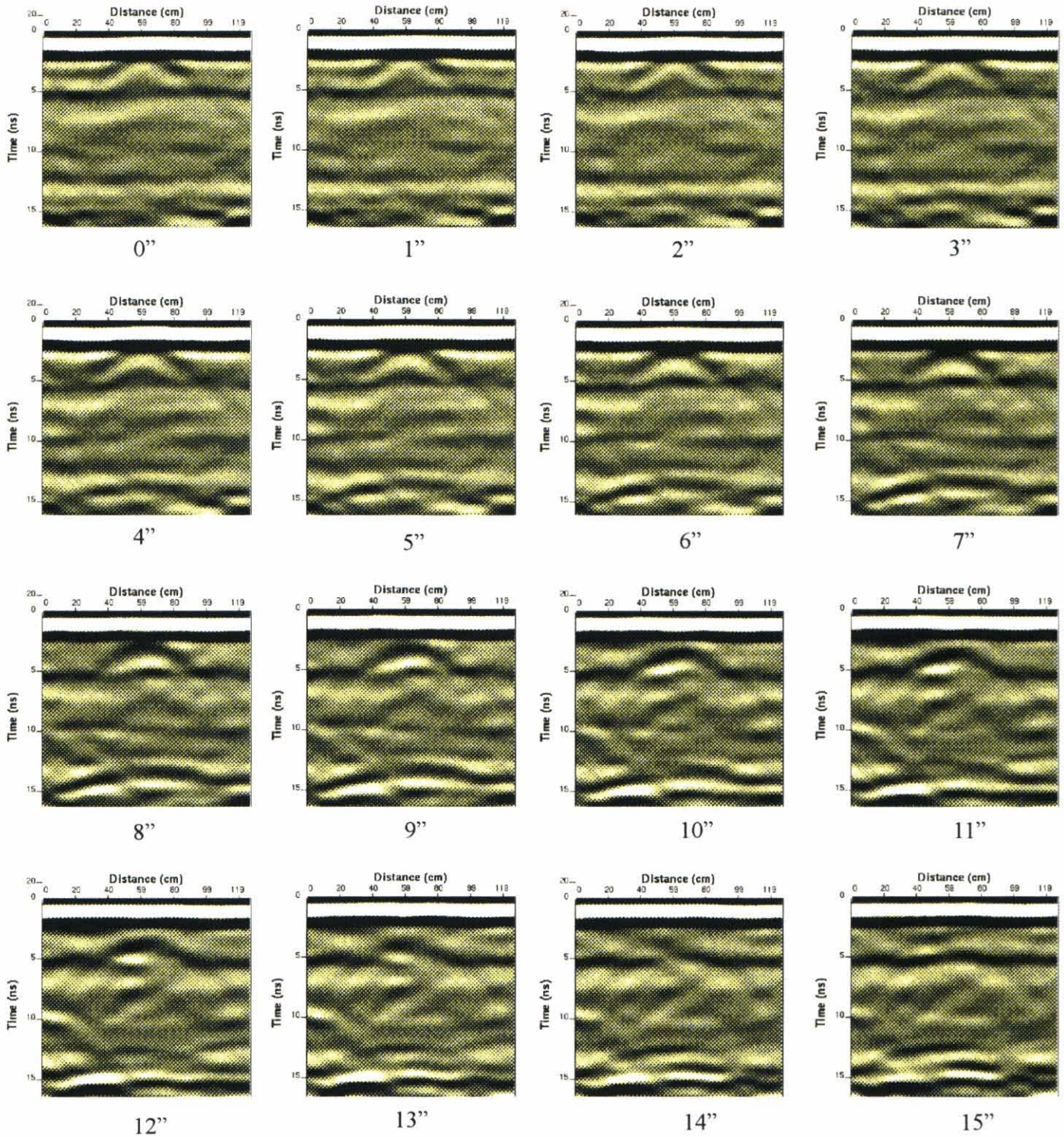
2csx: Small conductor buried at 2 feet.





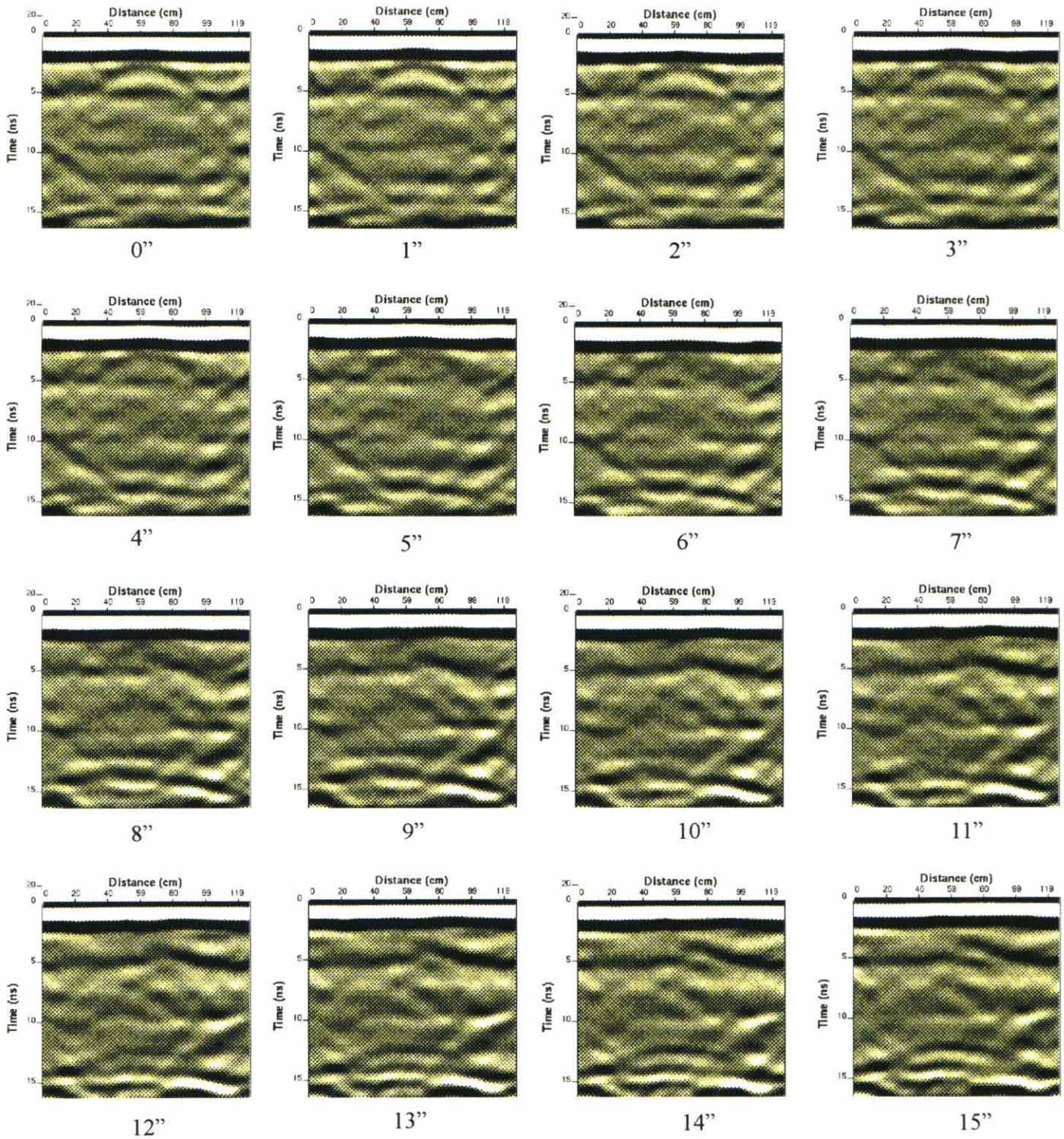
1dl: Large dielectric buried at 1 foot.





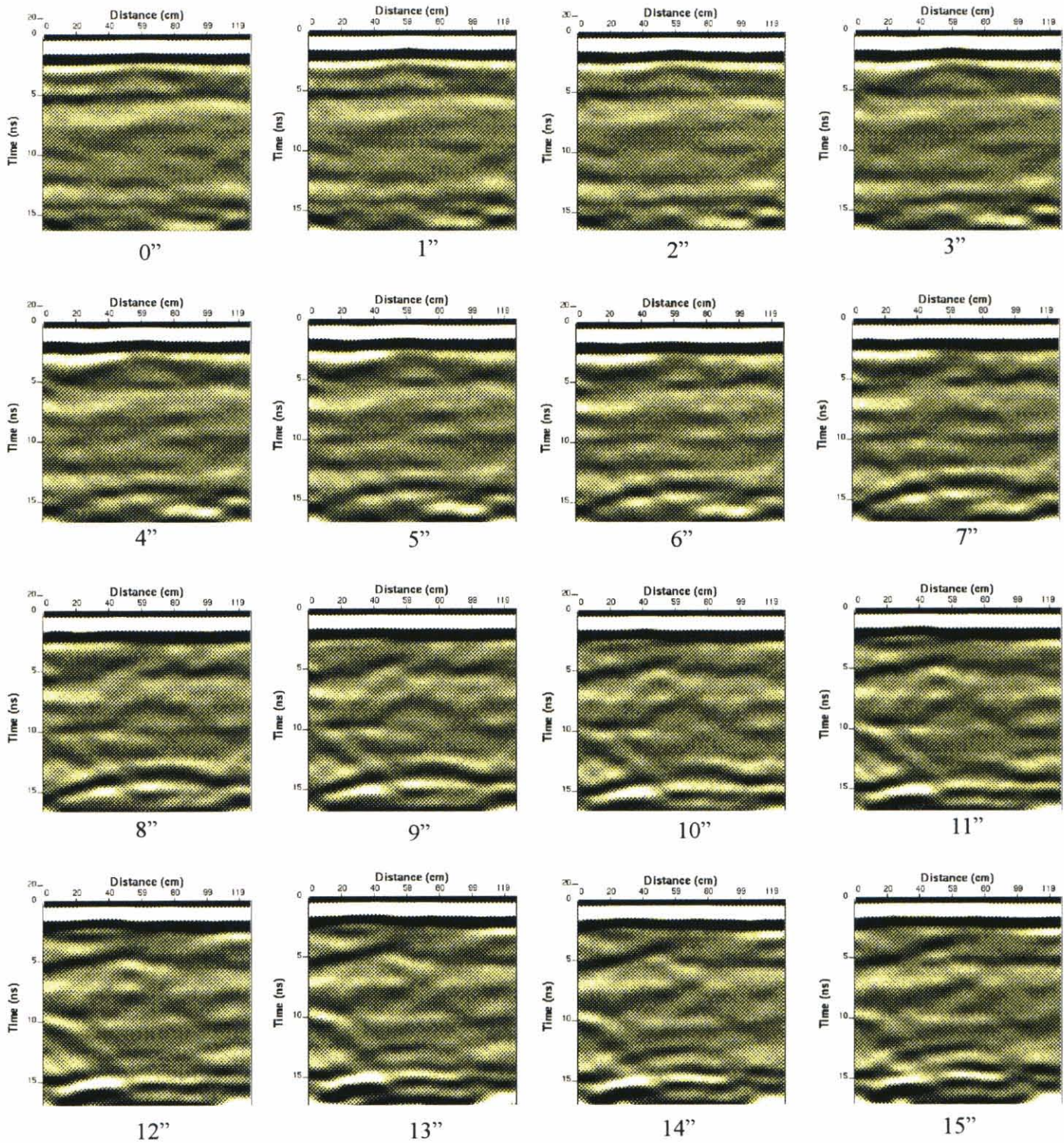
1dlx: Large dielectric buried at 1 foot.





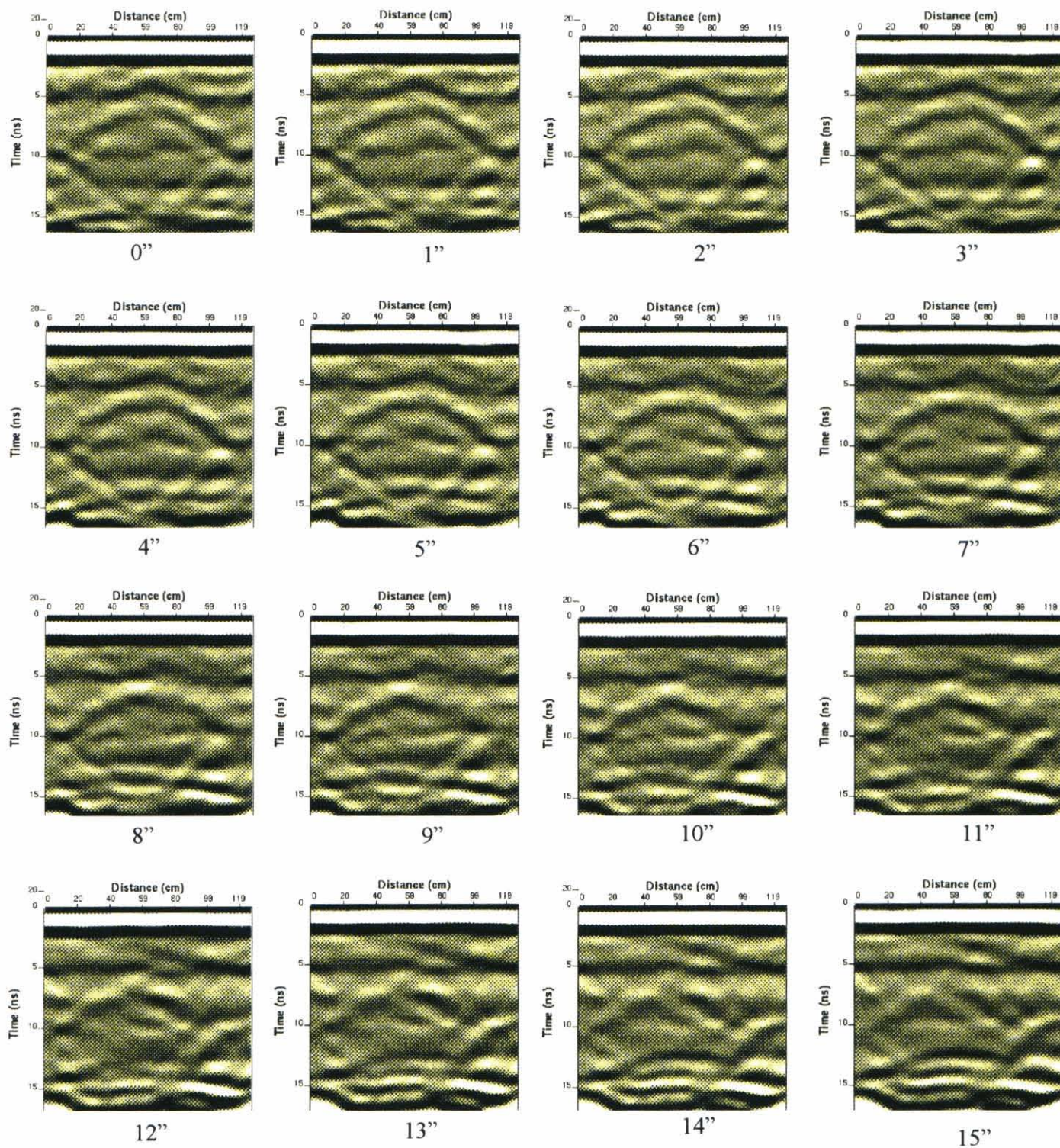
1dm: Medium dielectric buried at 1 foot.





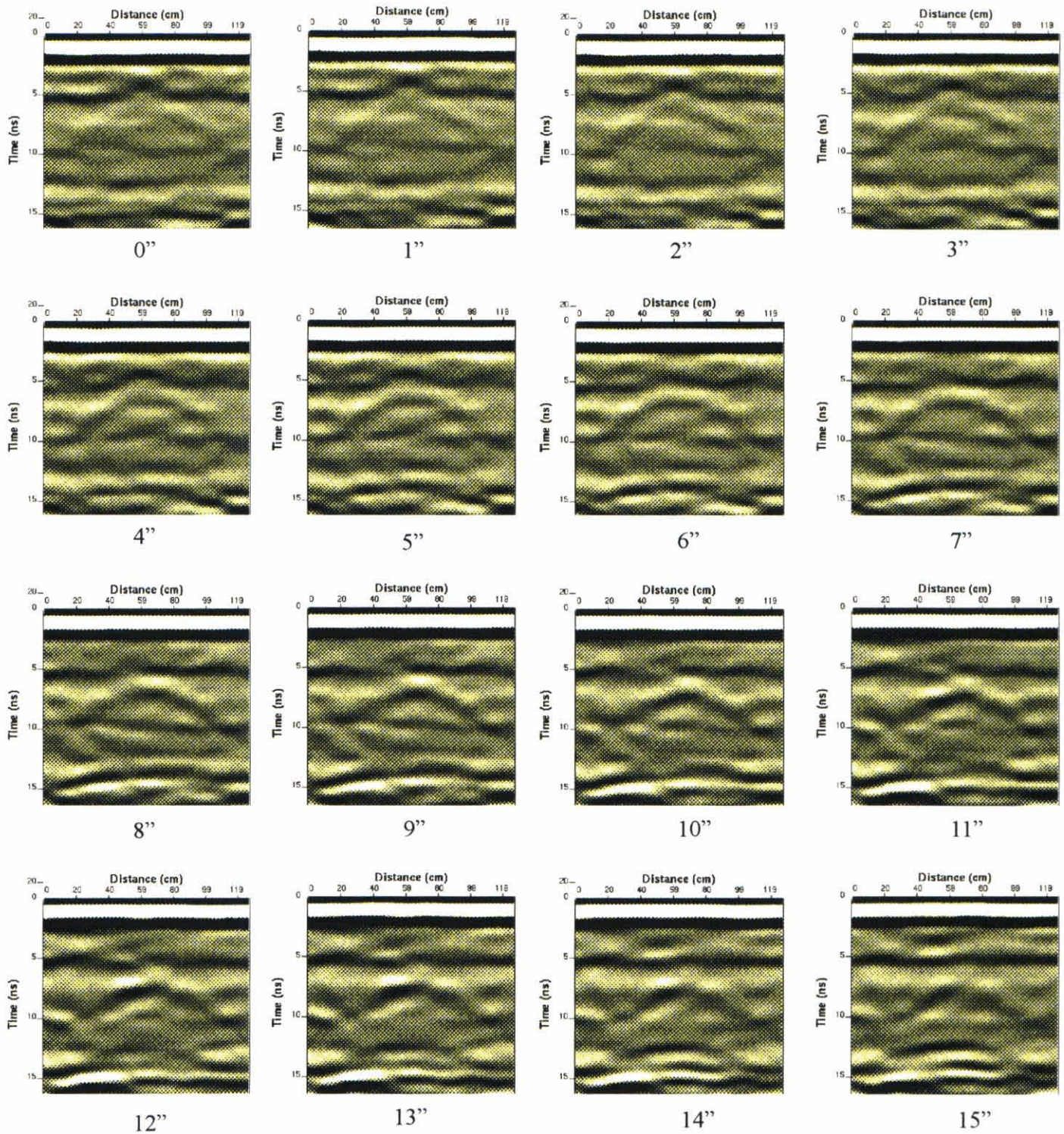
1dmx: Medium dielectric buried at 1 foot





2dl: Large dielectric buried at 2 feet.

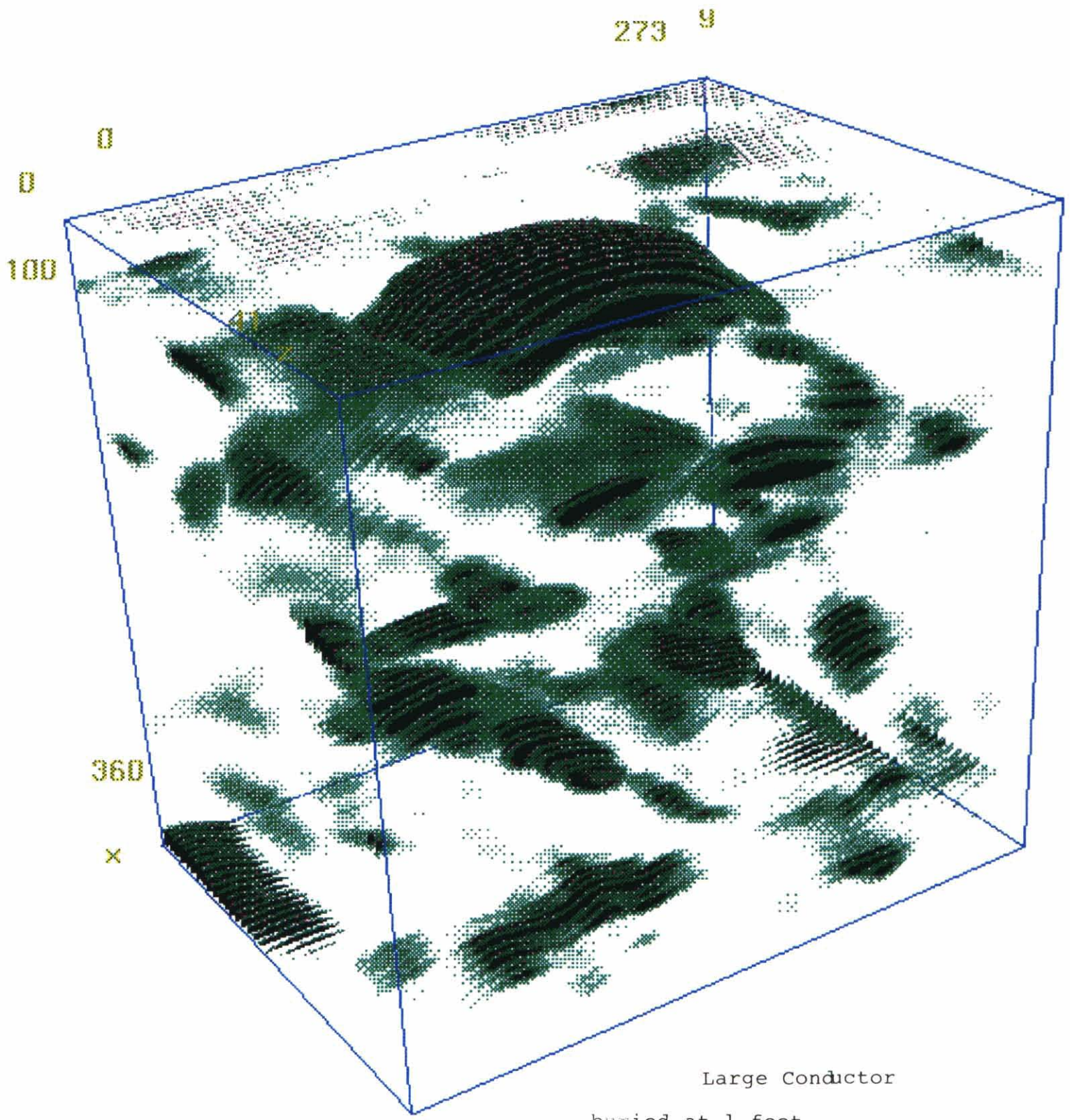


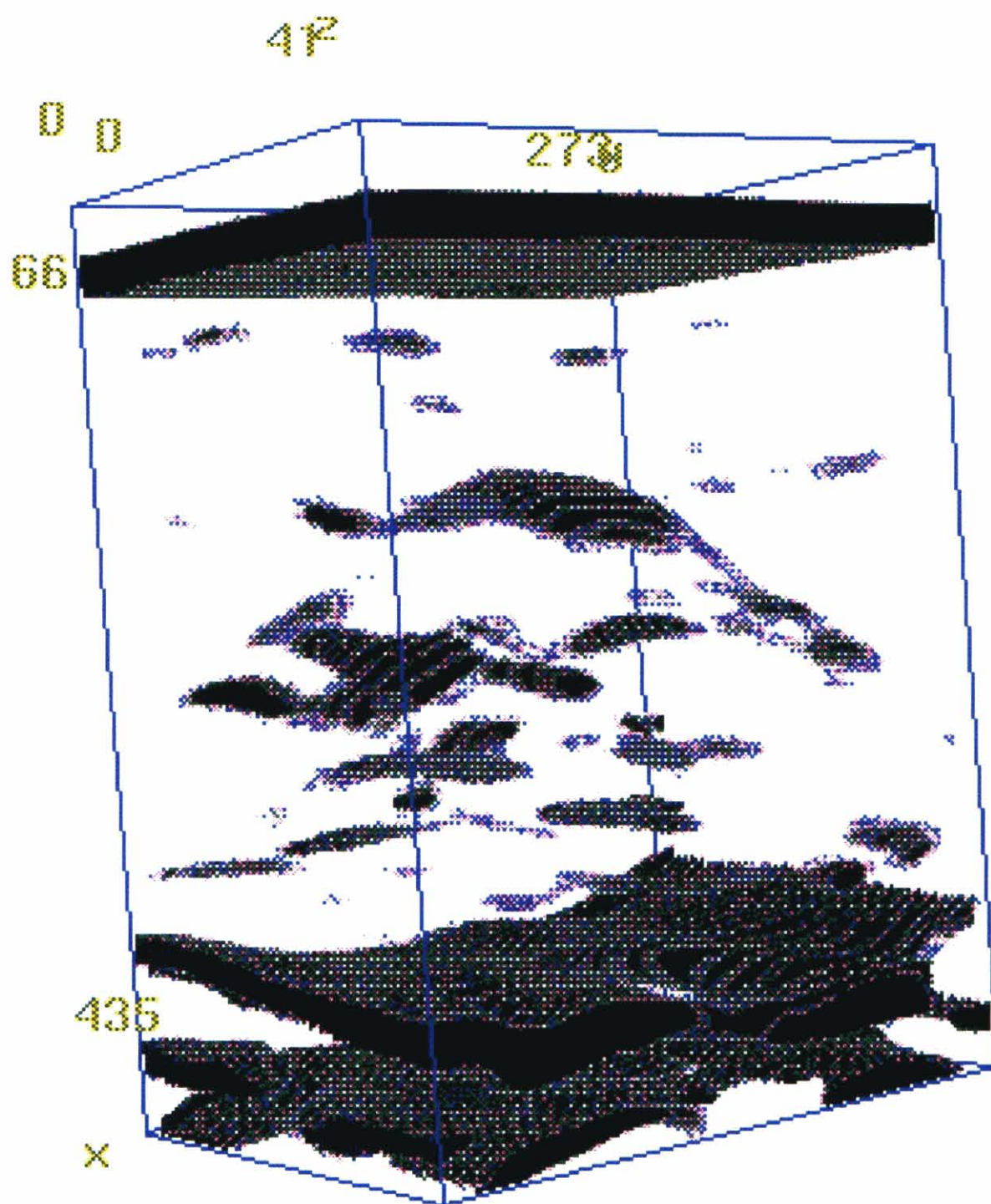


2dlx: Large dielectric buried at 2 feet.

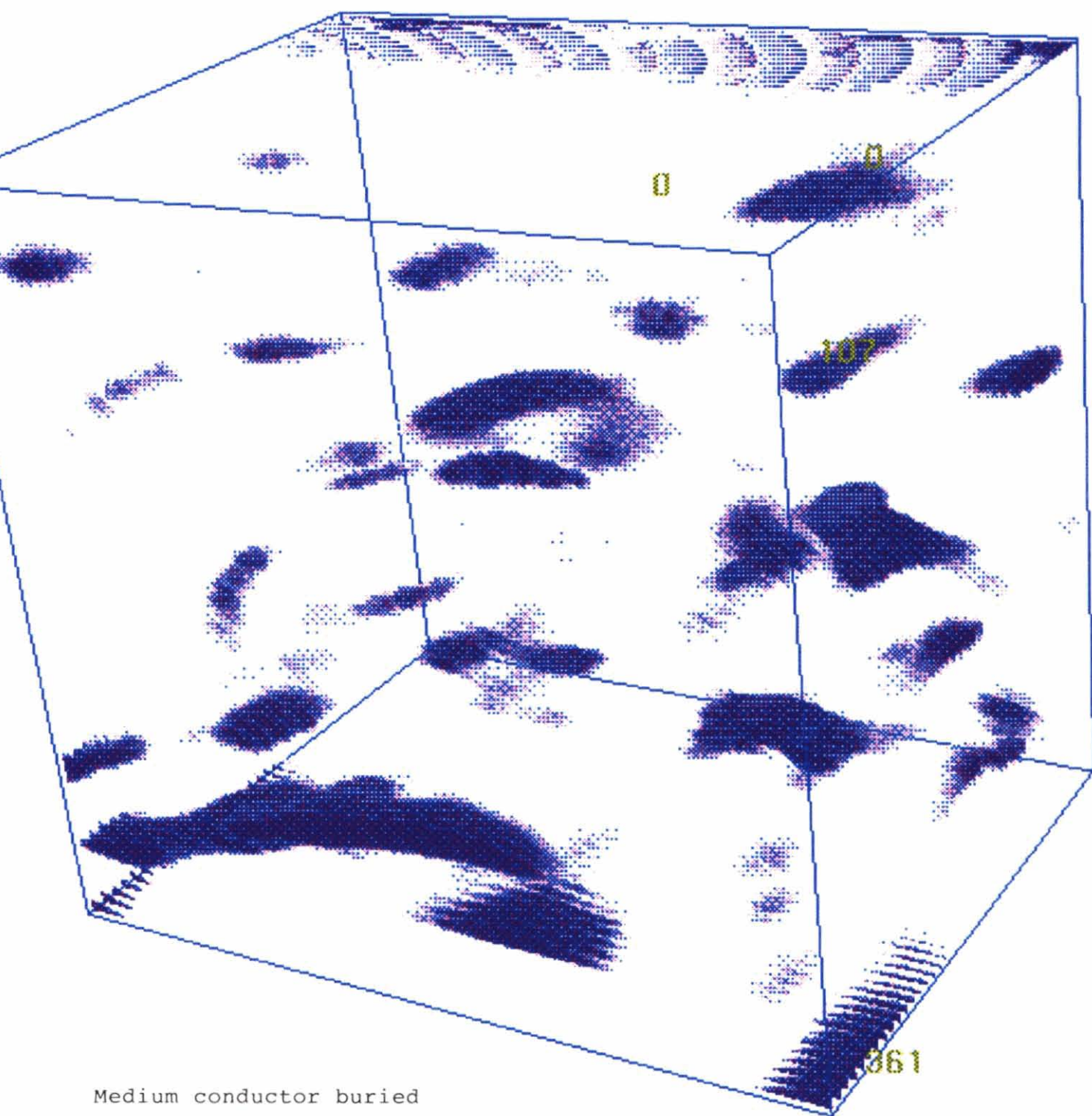


Appendix C



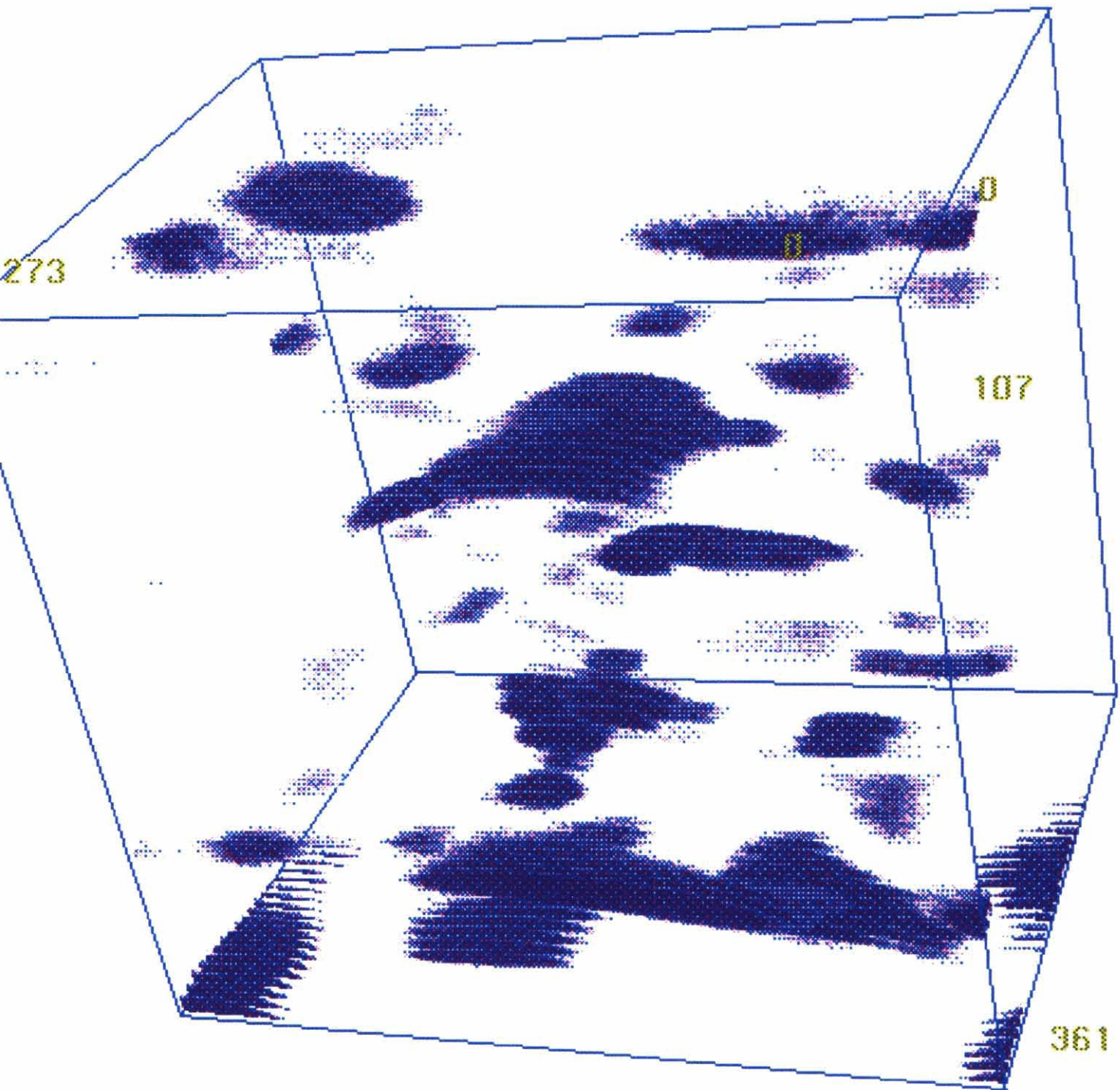


Large conductor buried
at 2 feet.



Medium conductor buried
at 2 feet.

2
41



Medium conductor buried at 2 feet
Antennas parallel to traverse

X

References

- Daniels, J.J., 1994, Ground Penetrating Radar for Engineering Applications, ASCE Special Volume on Geophysical Methods ASCE Publication ISSMFE#10, XIII ICSMFE, New Dehli, 1994.
- Daniels, J.J., Grumman, D., and Vendl, M., 1997, Vertical Incident Three Dimensional GPR: Jour. Env. Eng. Geoph., V.2, No.2, p1-9.
- Roberts, R.L., 1994, Analysis and Theoretical Modeling of GPR Polarization Data: Ph.D. Dissertation, The Ohio State University, Columbus, Oh.